



Cryptographic algorithms

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COSIC

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Outline (2)

- 4. Networking protocols
 - email, web, IPsec, SSL/TLS
- 5. New developments in cryptology
- 6. Cryptography best practices
- 7. Hash functions

Definitions

Confidentiality		data	entities
Integrity	confidentiality	encryption	anonymity
Availability	authentication	data authentication	identification

Authorisation

Non-repudiation of origin, receipt

Contract signing

Notarisation and Timestamping

Don't use the word authentication without defining it

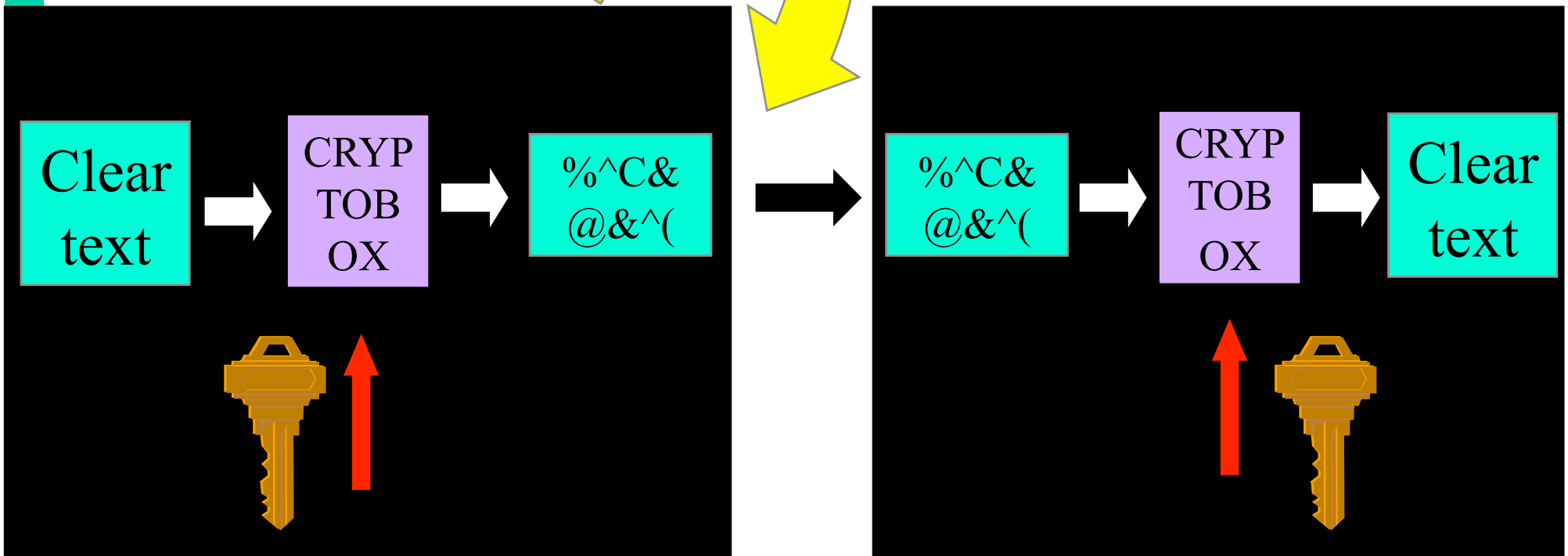
Cryptology: basic principles

Listen or Modify

Alice

Eve

Bob





Symmetric cryptology: confidentiality

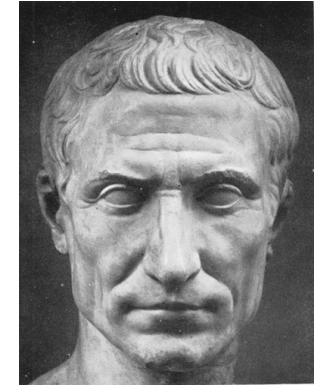
- old cipher systems:
 - transposition, substitution, rotor machines
- the opponent and her power
- the Vernam scheme
- DES and triple-DES
- AES
- RC4

Old cipher systems (pre 1900)

- Caesar cipher: shift letters over k positions in the alphabet (k is the secret key)

THIS IS THE CAESAR CIPHER

WKLV LV WKH FDHVDU FLSKHU



- Julius Caesar never changed his key ($k=3$).

Cryptanalysis example:

TIPGK RERCP JZJZJ WLE

UJQHL SFSDQ KAKAK XMF

VKRIM TGTER LBLBL YNG

WLSJN UHUF S MCMCM ZOH

XDTKO VOVGT NDNDN API

YNULP WKWHU OEEOE BQJ

ZOVMQ KXXIV PFPFP CRK

APWNR YLYJW QGQGQ DSL

BQXOS ZMXKX RHRHR ETM

CRYPT ANALY SISIS FUN

DSZQU BOBMZ TJTJT GVO

ETARV CPCNA UKUKU HWP

FUBSW DQDOB VLVLV IXQ

GVCTX EREPC WMWMW JYR

HWDUY FSFQD XNXNX KZS

IXEVZ GTGRE YOYOY LAT

JYFWA HUHSF ZPZPZ MBU

KZGXB IVITG AQAQA NCV

LAHYC JWJUH BRBRB ODW

MBIZD KXKVI CSCSC PEX

NCJAE LYLWJ DTD TD QFY

ODKBF MZMXK EUEUE RGZ

PELCG NANYL FVFVF SHA

QFMDH OBOZM GWGWG TIB

RGNEI PCPAN HXHXH UJC

SHOFJ QDQBO IYIYI VKD

Plaintext?

$k = 17$

Old cipher systems (pre 1900) (2)

- Substitutions

- ABCDEFGHIJKLMNOPQRSTUVWXYZ

- MZLNJSOAXFQGYKHLUCTDVWBI
PER

TRANS

ORIS

- Transpositions

POSITIONS

NOTIT

OSAN
P

! Easy to
break using
statistical
techniques

Security

- there are $n!$ different substitutions on an alphabet with n letters
- there are $n!$ different transpositions of n letters
- $n=26$: $n!=403291461126605635584000000 = 4 \cdot 10^{26}$ keys
- trying all possibilities at 1 nanosecond per key requires....

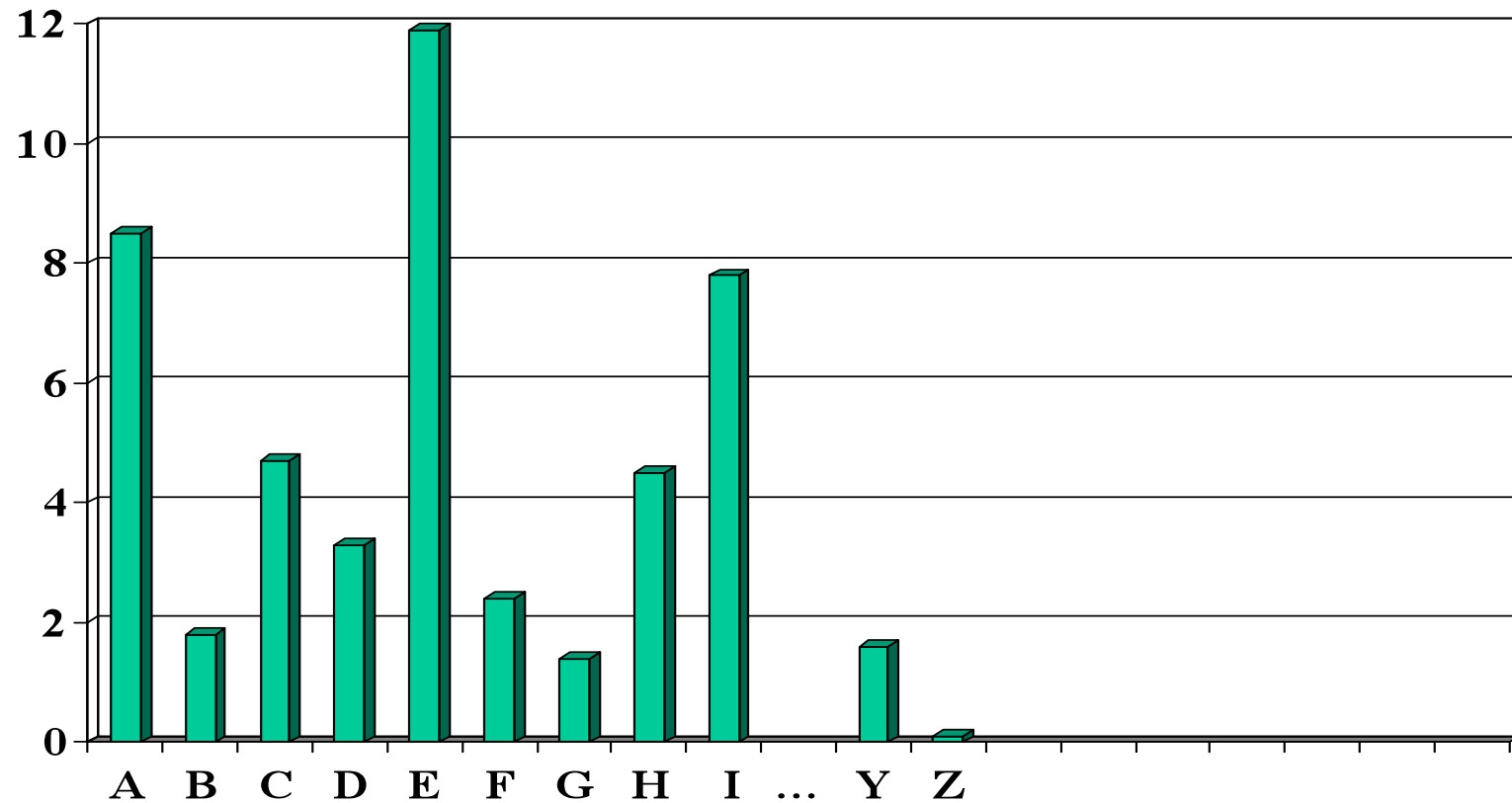
$$4 \cdot 10^{26} / (10^9 \cdot 10^5 \cdot 4 \cdot 10^2) = 10^{10} \text{ years}$$

keys per
second

seconds
per day

days per
year

Letter distributions

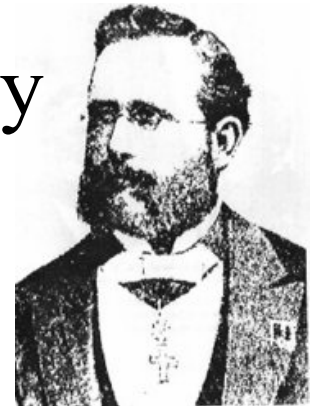


Assumptions on Eve (the opponent)

- A scheme is broken if Eve can deduce the key or obtain additional plaintext
- Eve can always **try all keys** till “meaningful” plaintext appears: a brute force attack
 - solution: large key space
- Eve will try to find **shortcut attacks** (faster than brute force)
 - history shows that designers are too optimistic about the security of their cryptosystems

Assumptions on Eve (the opponent)

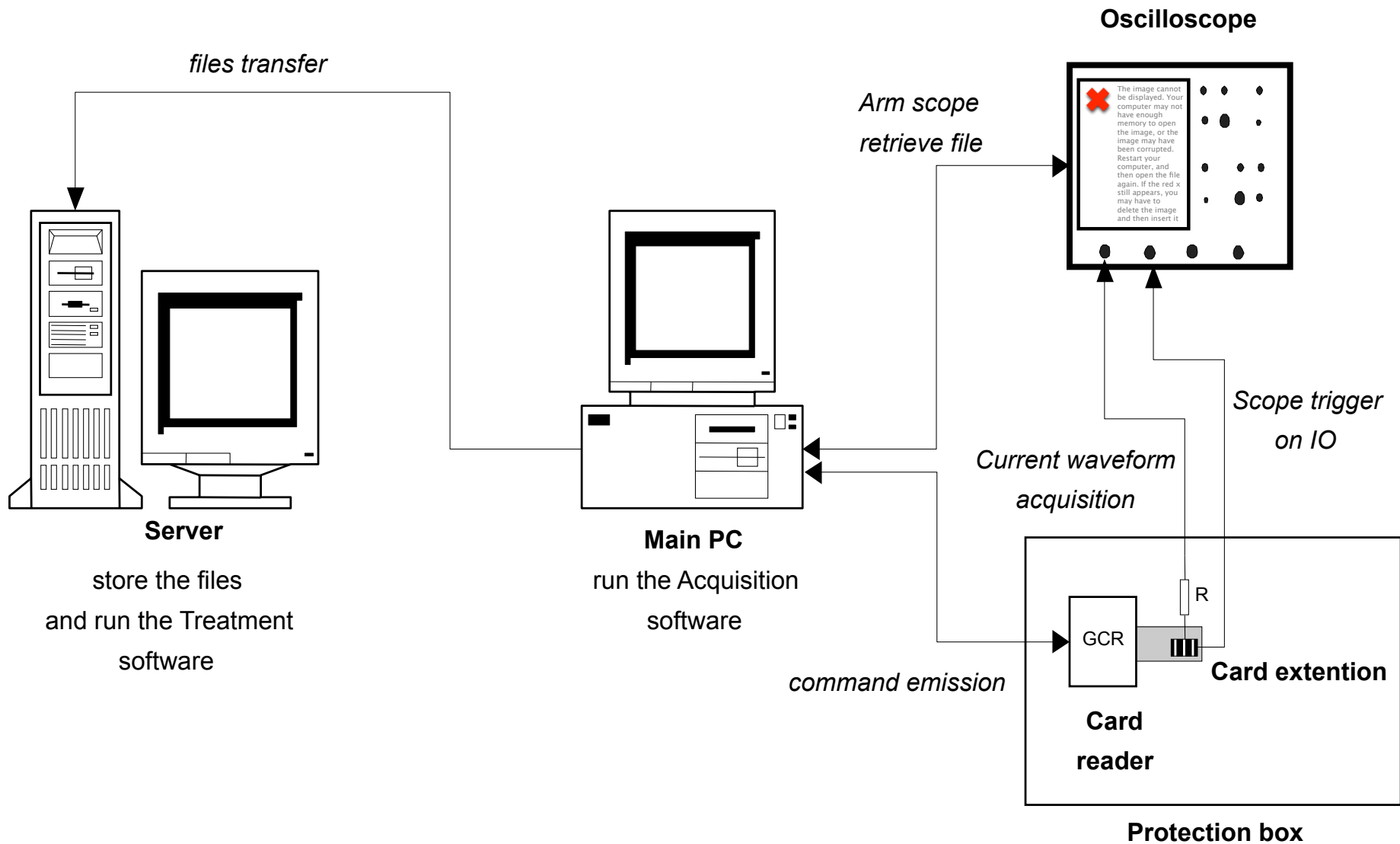
- Cryptology = cryptography + cryptanalysis
- Eve knows the algorithm, except for the key (Kerckhoffs's principle)
- increasing capability of Eve:
 - knows some information about the plaintext (e.g., in English)
 - knows part of the plaintext
 - can choose (part of) the plaintext and look at the ciphertext
 - can choose (part of) the ciphertext and look at the plaintext



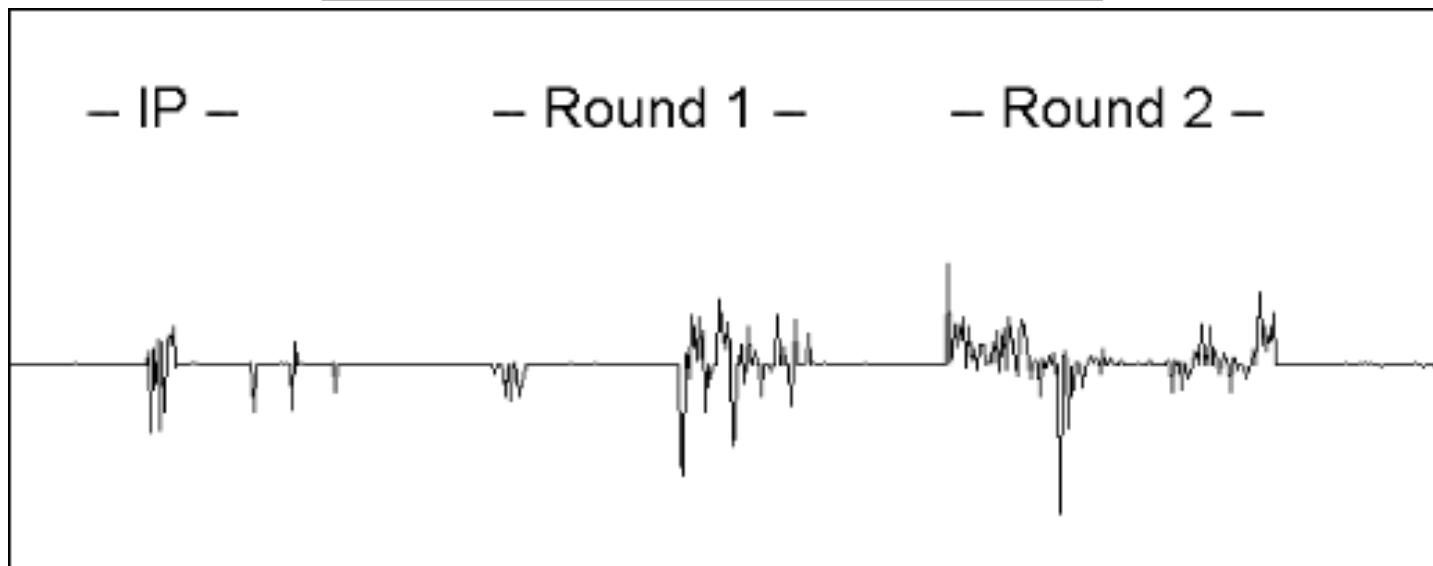
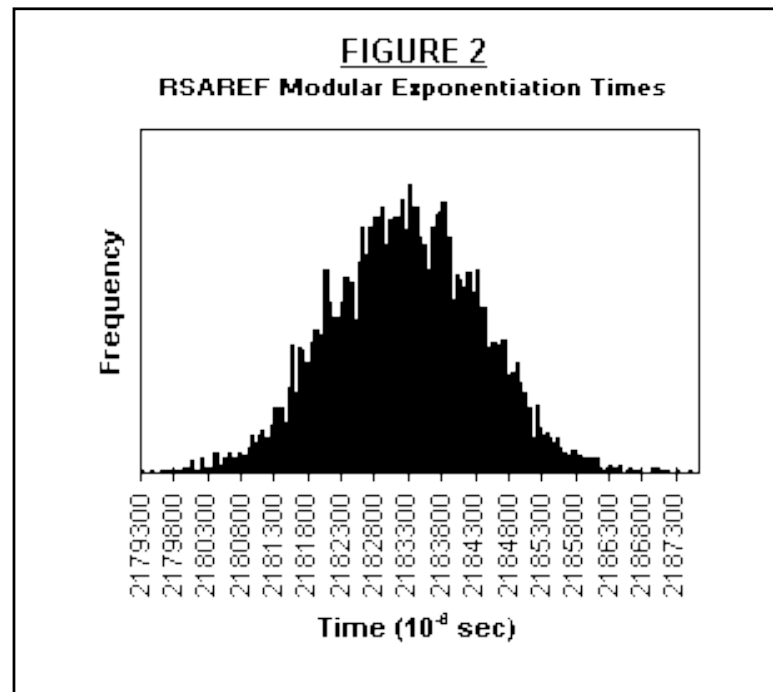
New assumptions on Eve

- Eve may have access to **side channels**
 - timing attacks
 - simple power analysis
 - differential power analysis
 - acoustic attacks
 - electromagnetic interference
- Eve may launch **(semi-)invasive attacks**
 - differential fault analysis
 - probing of memory or bus

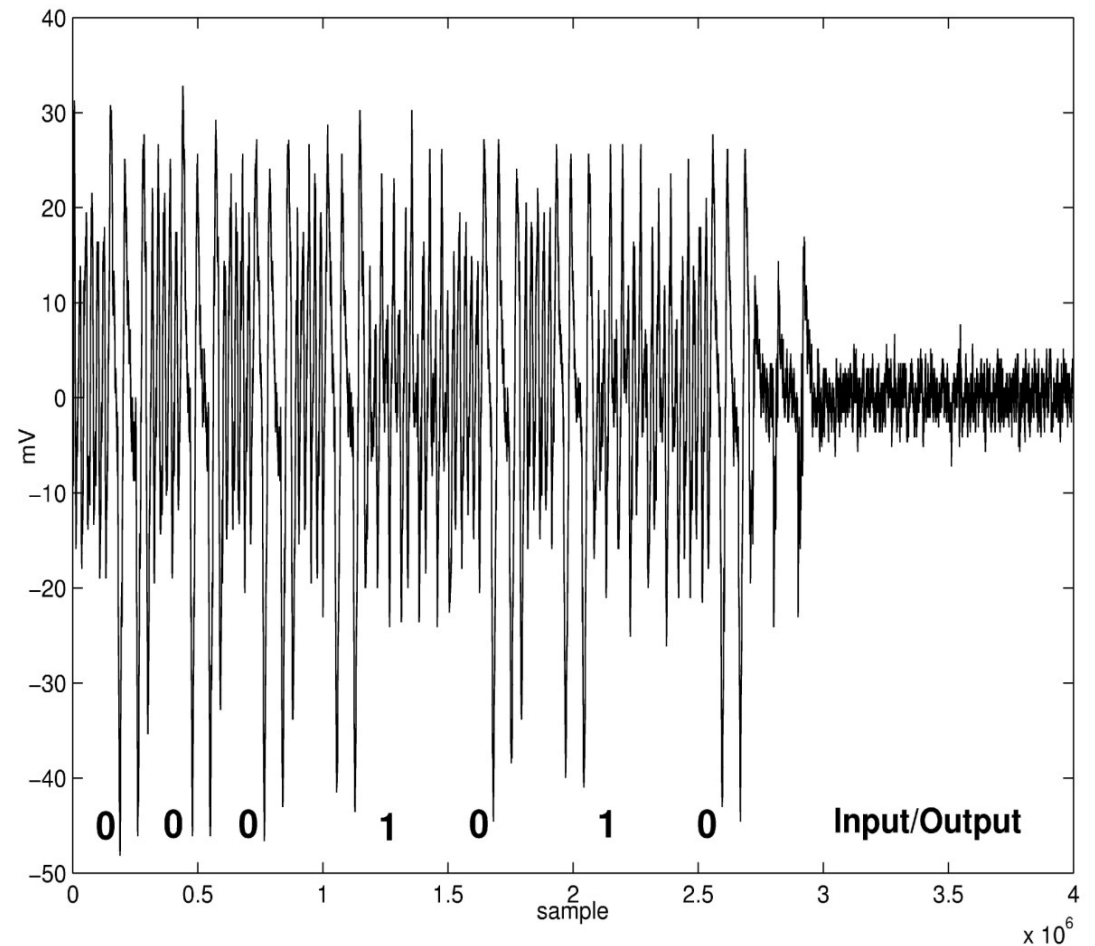
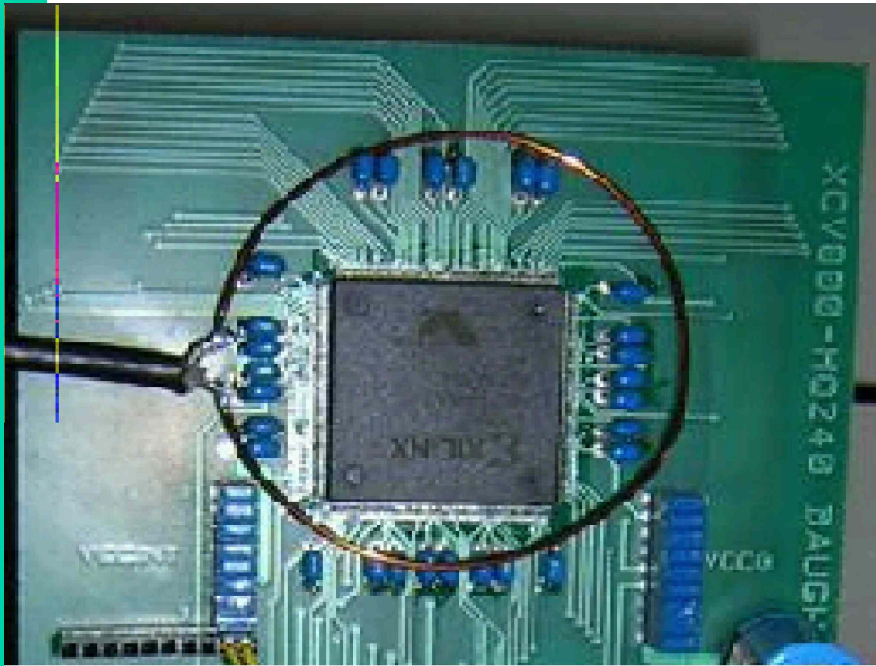
Side channel analysis



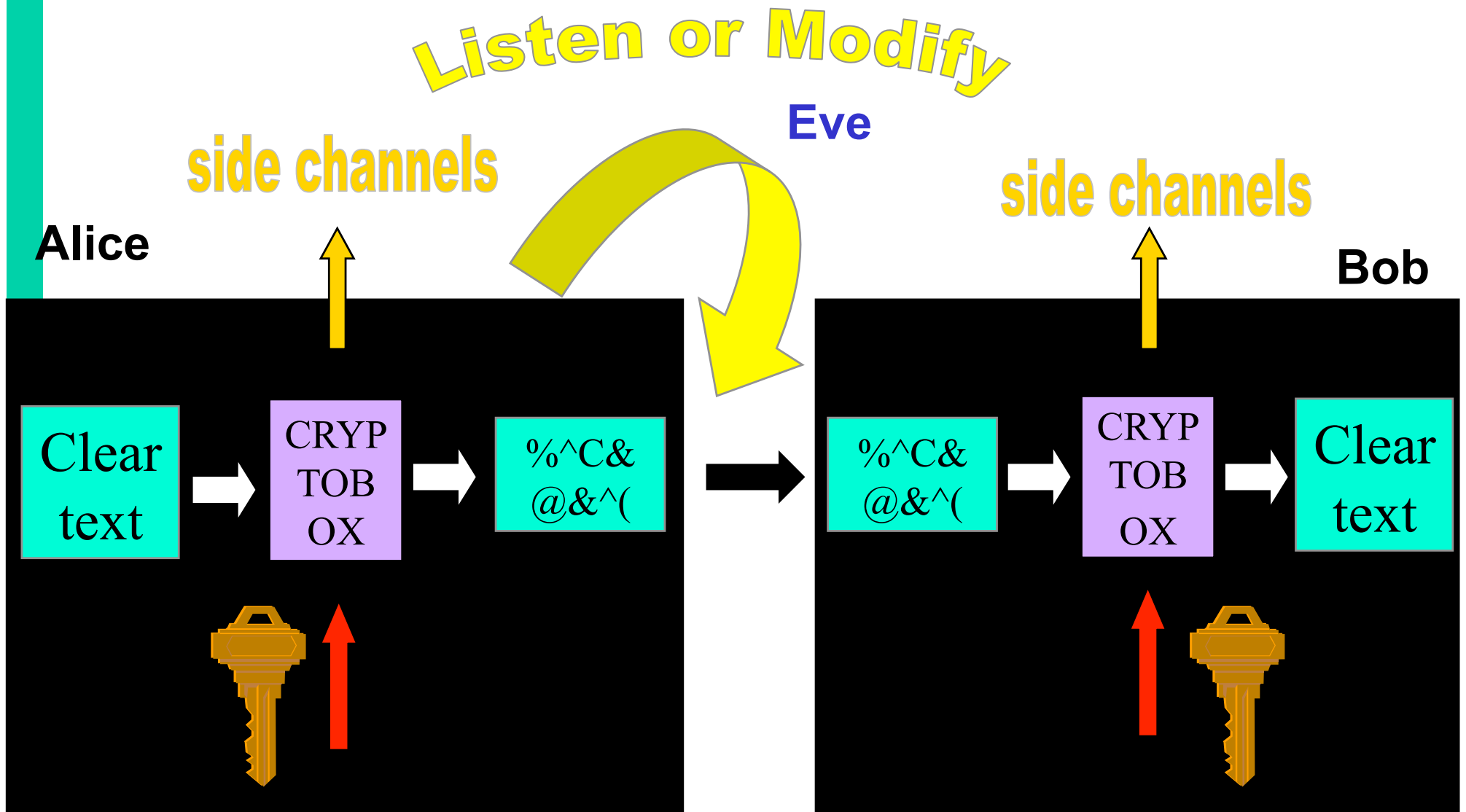
Timing attacks and power analysis



Side channel analysis: EMA



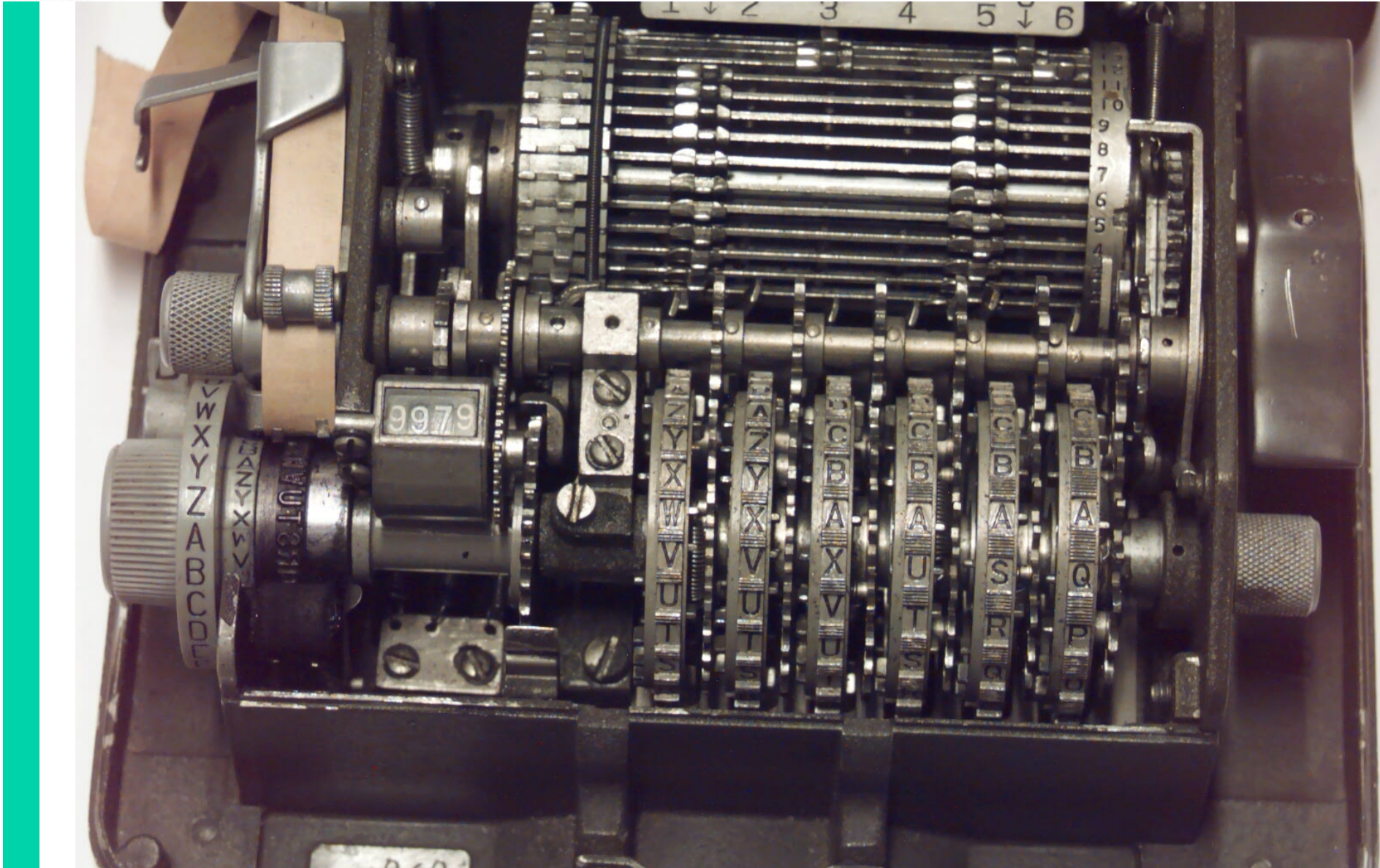
Cryptology + side channels





Boris Hagelin

Mechanical: Hagelin C38



Problem: what is this?

- Cryptogram [=14 January 1961 11.00 h]
- **<AHQNE XVAZW IQFFR JENFV OUXBD**
LQWDB BXFRZ NJVYB QVGOZ KFYQV
GEDBE HGMP S GAZJK RDJQC VJTEB
XNZZH MEVGS ANLLB DQCGF PWCVR
UOMWW LOGSO ZWVVV LDQNI YTZAA
OIJDR UEAAV RWYXH PAWSV CHTYN
HSUIY PKFPZ OSEAW SUZMY QDYEL
FUVOA WLSSD ZVKPU ZSHKK PALWB
SHXRR MLQOK AHQNE 11205
141100>

The answer

- Plaintext [=14 January 1961 11.00 h]

- **DOFGD** **VISWA** **WVISW** **JOSEP** **HWXXW**
TERTI **OWMIS** **SIONW** **BOMBO** **KOWVO**
IRWTE **LEXWC** **EWSUJ** **ETWAM** **BABEL**
GEWXX **WJULE** **SWXXW** **BISEC** **TWTRE**
SECVX **XWRWV** **WMWPR** **INTEX** **WXXWP**
RIMOW **RIENW** **ENVOY** **EWRUS** **URWWX**
XWPOU **VEZWR** **EGLER** **WXXWS** **ECUND**
OWREP **RENDR** **EWDUR** **GENCE** **WPLAN**
WBRAZ **ZAWWC**

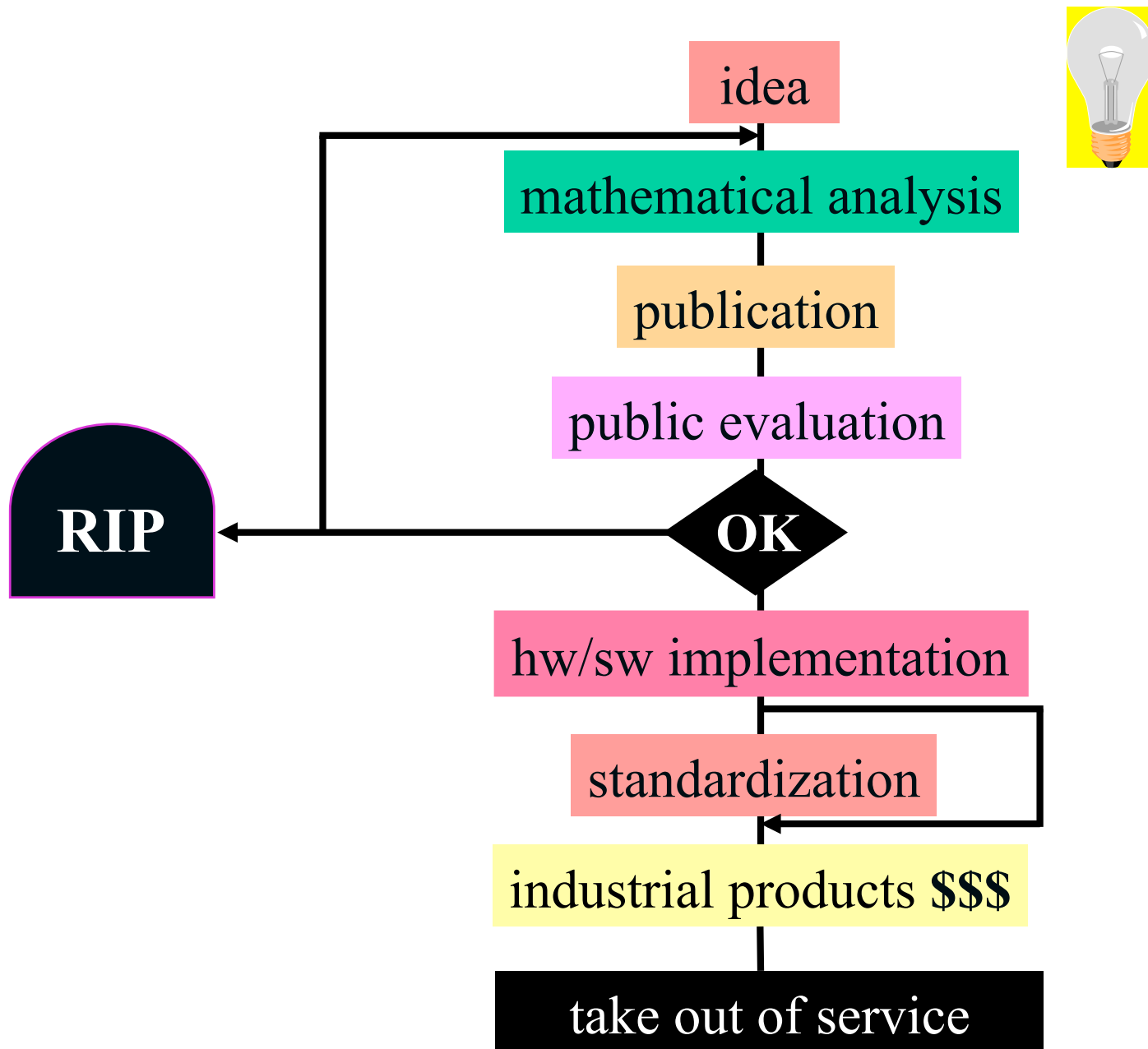
The answer (in readable form)

- Plaintext [=14 January 1961 11.00 h]
- TRESECV. R V M PRINTEX. PRIMO
RIEN ENVOYE RUSUR. POUVEZ
REGLER. SECUNDO REPRENDRE
DURGENCE PLAN BRAZZA VIS A VIS
JOSEP H. TERTIO MISSION
BOMBOKO VOIR TELEX CE SUJET
AMBABELGE. JULES.

The Rotor machines (WW II)



Life cycle of a cryptographic algorithm



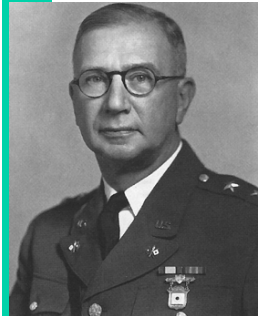


Vernam scheme

(1917)

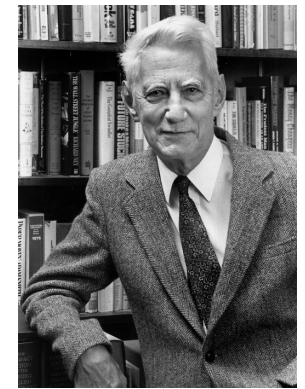
Mauborgne: one time pad

(1917+x)

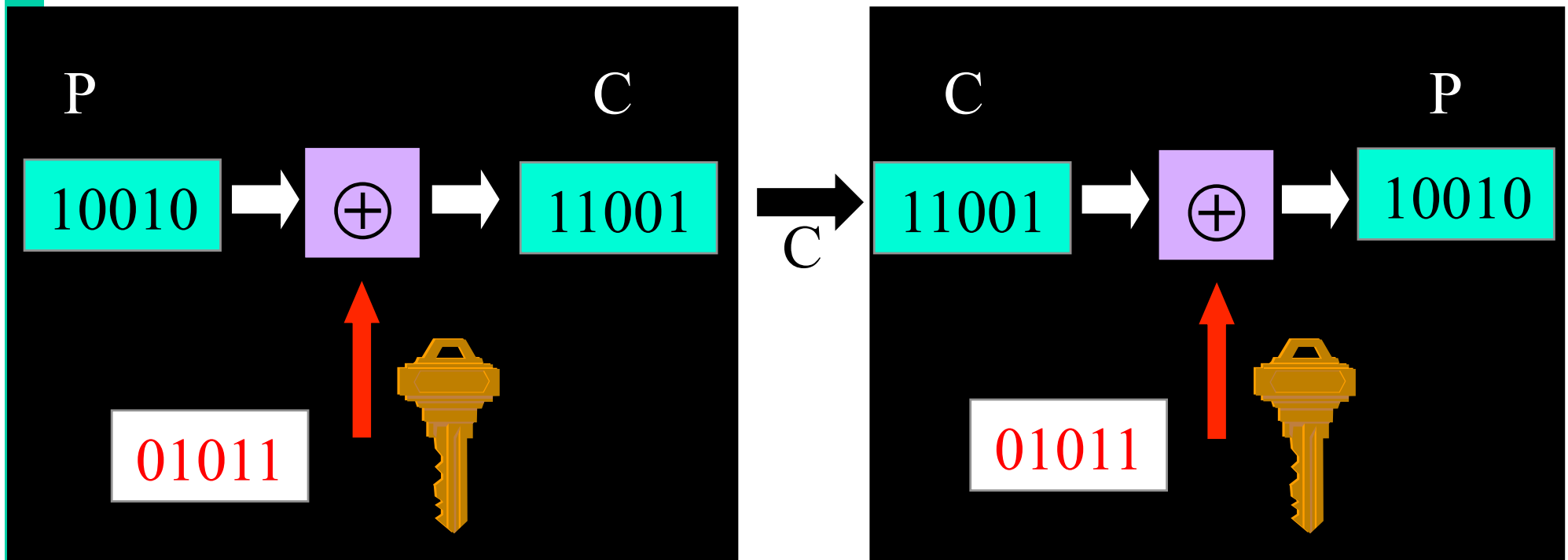


Shannon

(1948)

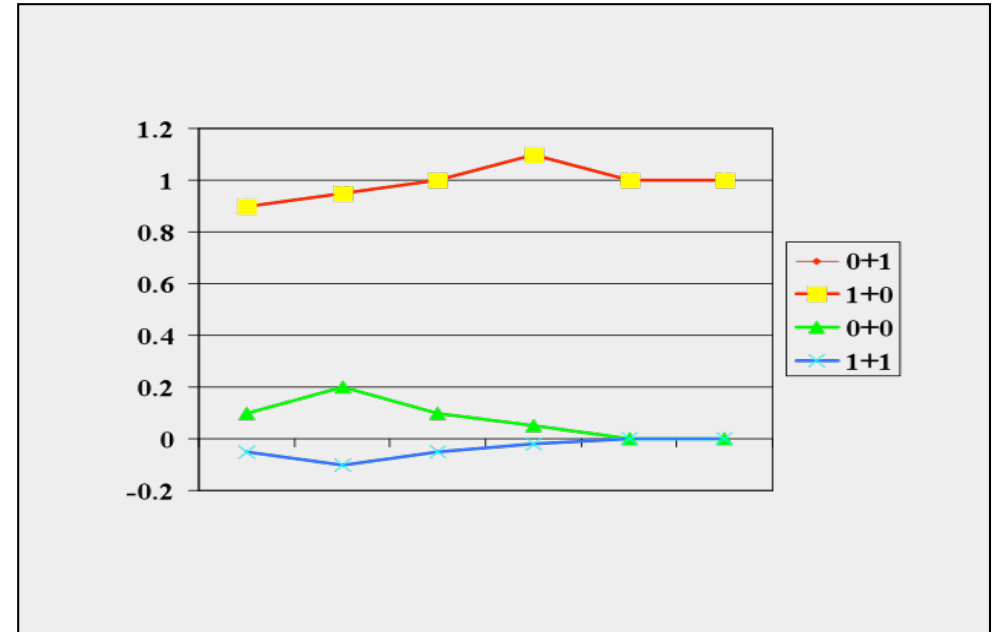


key is random string, as long as the plaintext
information theoretic proof of security



Vernam scheme

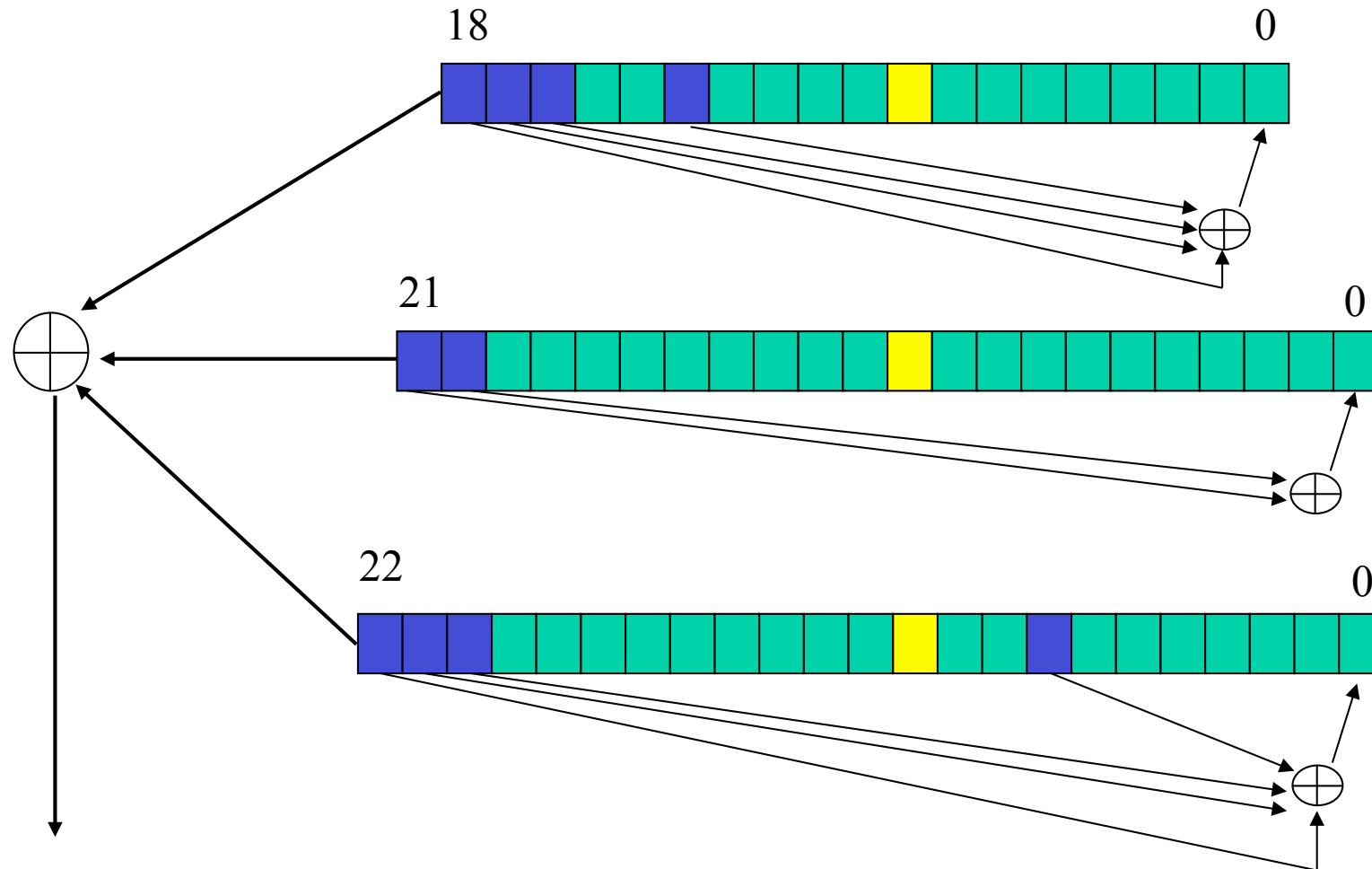
- $0 + 1 = 1$
 - $1 + 0 = 1$
 - $0 + 0 = 0$
 - $1 + 1 = 0$
-
- identical mathematical symbols can result in different electrical signals



Three approaches in cryptography

- **information theoretic** security
 - ciphertext only
 - part of ciphertext only
 - noisy version of ciphertext
- **system-based** or practical security
 - also known as “prayer theoretic” security
- **complexity theoretic** security:
 - model of computation, definition, proof
 - variant: quantum cryptography

A5/1 stream cipher (GSM)



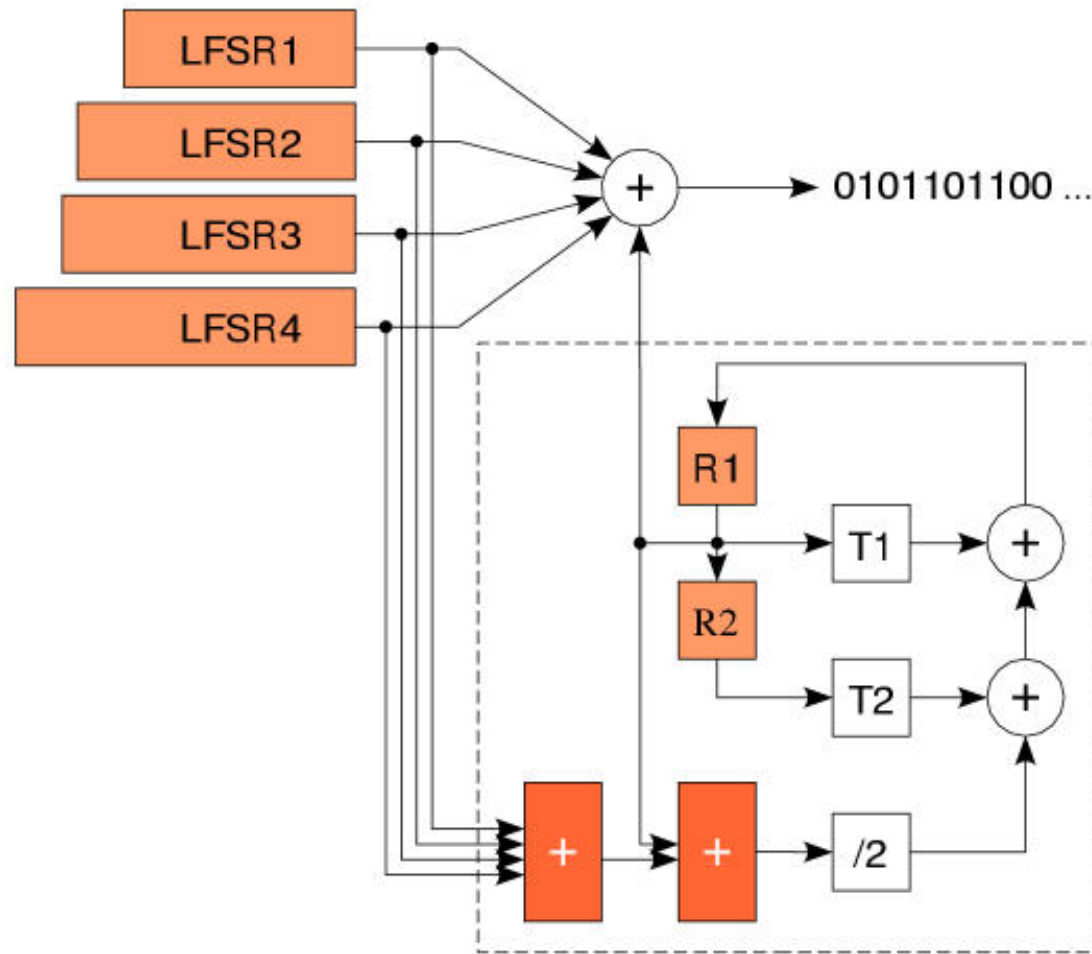
Clock control: registers agreeing with majority are clocked (2 or 3) ■

A5/1 stream cipher (GSM)

A5/1 attacks

- exhaustive key search: 2^{64} (or rather 2^{54})
 - Hardware 10K\$ < 1 minute ciphertext only
- search 2 smallest registers: 2^{45} steps
- [BWS00] 1 minute on a PC
 - 2 seconds of known plaintext
 - 2^{48} precomputation, 146 GB storage
- [BB05]: 10 minutes on a PC,
 - 3-4 minutes of **ciphertext only**

Bluetooth stream cipher



brute force: 2^{128} steps

[Lu+05] 24 known bits of 2^{24} frames, 2^{38} computations, 2^{33} memory

A simple cipher: RC4 (1987)



- designed by Ron Rivest (MIT)
- leaked in 1994
- **S[0..255]**: secret table derived from user key K

for $i=0$ to 255 $S[i]:=i$

$j:=0$

for $i=0$ to 255

$j:=(j + S[i] + K[i]) \bmod 256$

swap **S[i]** and **S[j]**

$i:=0, j:=0$

A simple cipher: RC4 (1987)

Generate key stream which is added to plaintext

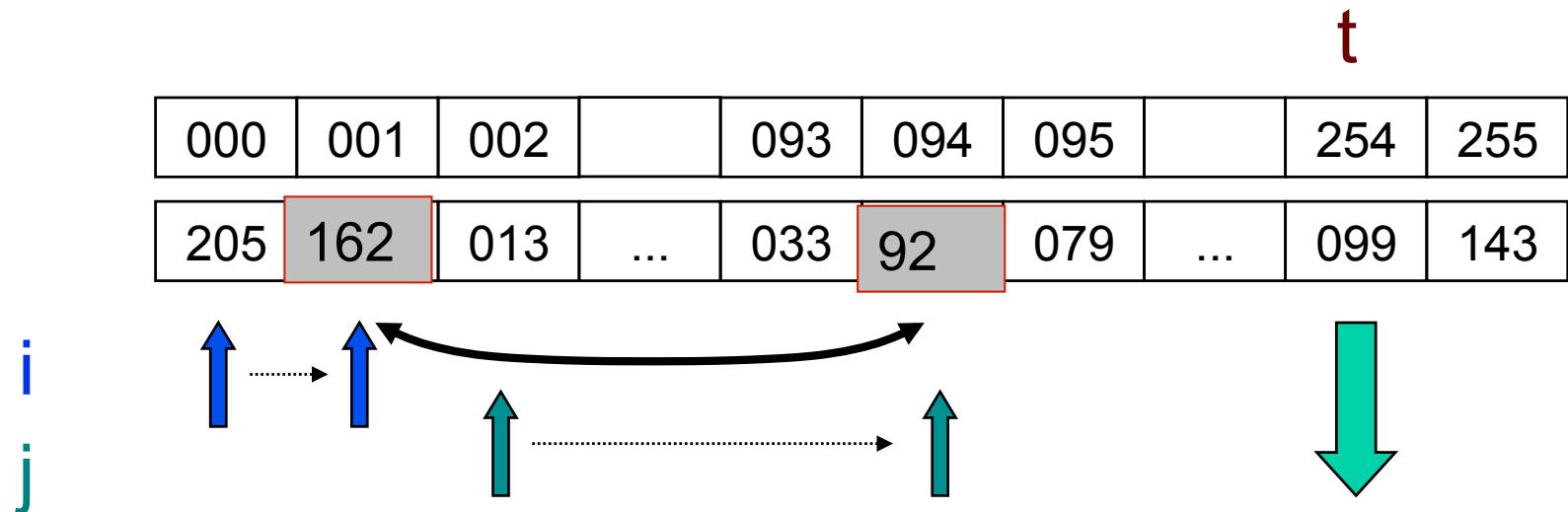
$i := i + 1$

$j := (j + S[i]) \bmod 256$

swap $S[i]$ and $S[j]$

$t := (S[i] + S[j]) \bmod 256$

output $S[t]$



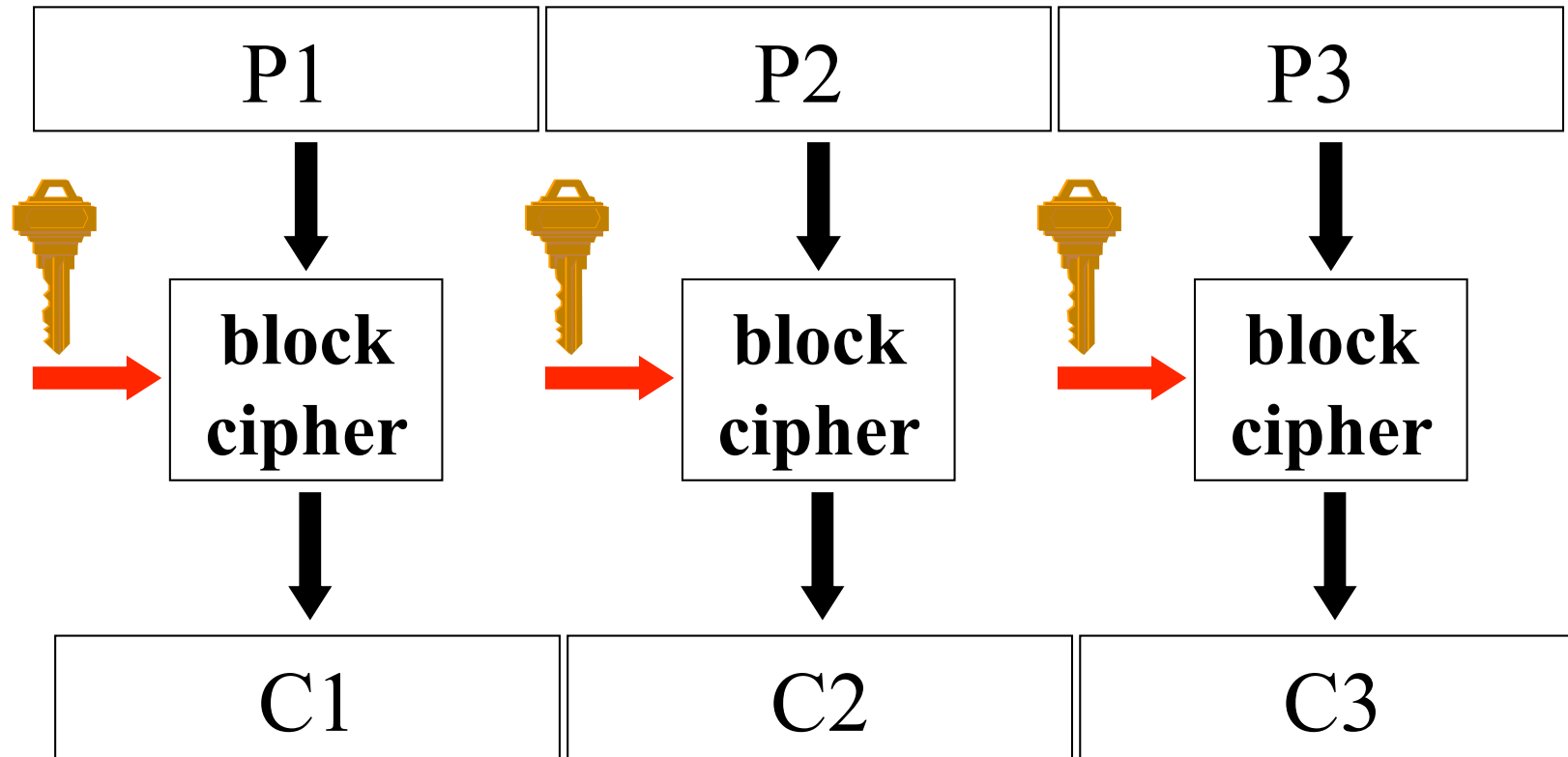
RC4: weaknesses

- often used with 40-bit key
 - US export restrictions until Q4/2000
- best known general shortcut attack: 2^{241}
- weak keys and key setup (shuffle theory)
- some statistical deviations
 - e.g., 2nd output byte is biased
 - solution: drop first 256 bytes of output
- problem with resynchronization modes (WEP)

Block cipher

- large table: list n-bit ciphertext for each n-bit plaintext
 - if n is large: very secure (codebook)
 - but for an n-bit block: 2^n values
 - impractical if $n \geq 32$
- alternative $n = 64$ or 128
 - simplify the implementation
 - repeat many simple operations

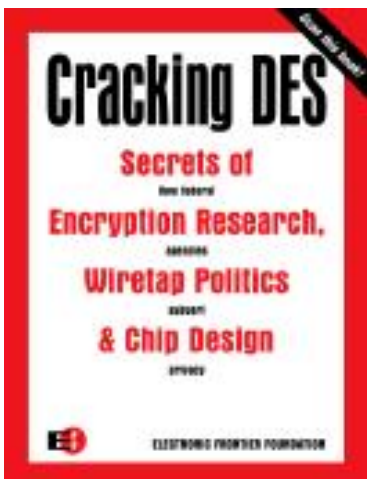
Block cipher (2)



- larger data units: 64...128 bits
- memoryless
- repeat simple operation (round) many times

Data Encryption Standard (1977)

- encrypts 64 plaintext bits under control of a 56-bit key
- 16 iterations of a relatively simple mapping
- FIPS: US government standard for sensitive but unclassified data
- worldwide de facto standard since early 80ies
- surrounded by controversy



Security of DES (56 bit key)

- PC: trying 1 DES key: 15 ns
- Trying all keys on 250 PCs:
1 month: $2^{26} \times 2^{16} \times 2^5 \times 2^8 = 2^{55}$
- M. Wiener's design (1993):
1,000,000 \$ machine: 3 hours
(in 2010: 5 seconds)



EFF Deep Crack (July 1998)

250,000 \$ machine: 50 hours...

DES: security (ct'd)

- Moore's "law": speed of computers doubles every 18 months
 - key lengths need to grow in time
- Use new algorithms with longer keys
 - adding 1 key bits doubles the work for the attacker
- Key length recommendations in 2009
 - < 64 bits: insecure
 - 80 bits: 3-5 years
 - 100 bits: 20-25 years

Federal Register, July 24, 2004

DEPARTMENT OF COMMERCE

National Institute of Standards and Technology

[Docket No. 040602169– 4169– 01]

Announcing Proposed Withdrawal of Federal Information Processing Standard (FIPS) for the Data Encryption Standard (DES) and Request for Comments

AGENCY: National Institute of Standards and Technology (NIST), Commerce.

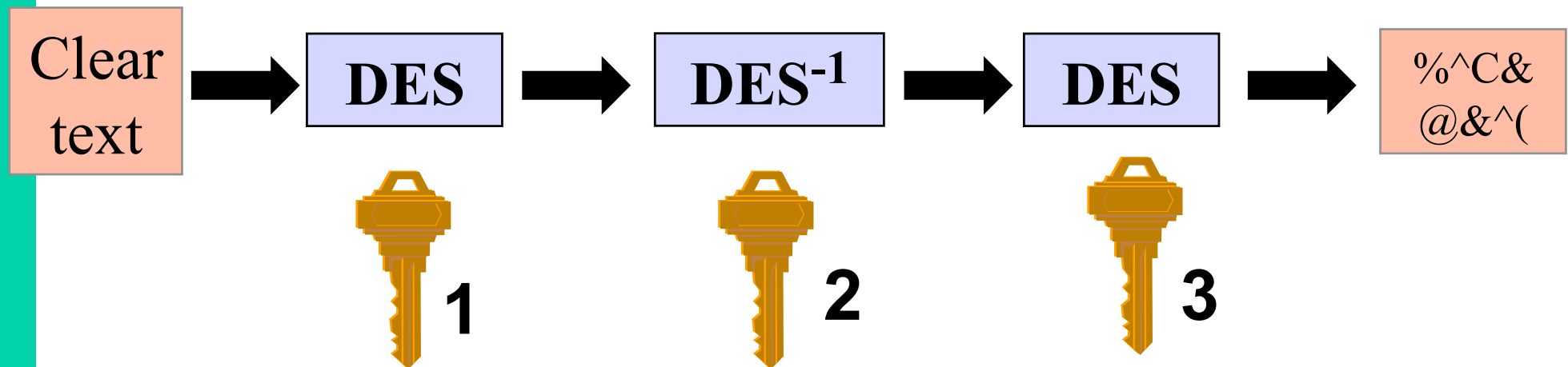
ACTION: Notice; request for comments.

- **SUMMARY:** The Data Encryption Standard (DES), currently specified in Federal Information Processing Standard (FIPS) 46–3, was evaluated pursuant to its scheduled review. At the conclusion of this review, **NIST determined that the strength of the DES algorithm is no longer sufficient to adequately protect Federal government information.** As a result, NIST proposes to withdraw FIPS 46–3, and the associated FIPS 74 and FIPS 81. Future use of DES by Federal agencies is to be permitted only as a component function of the Triple Data Encryption Algorithm (TDEA).

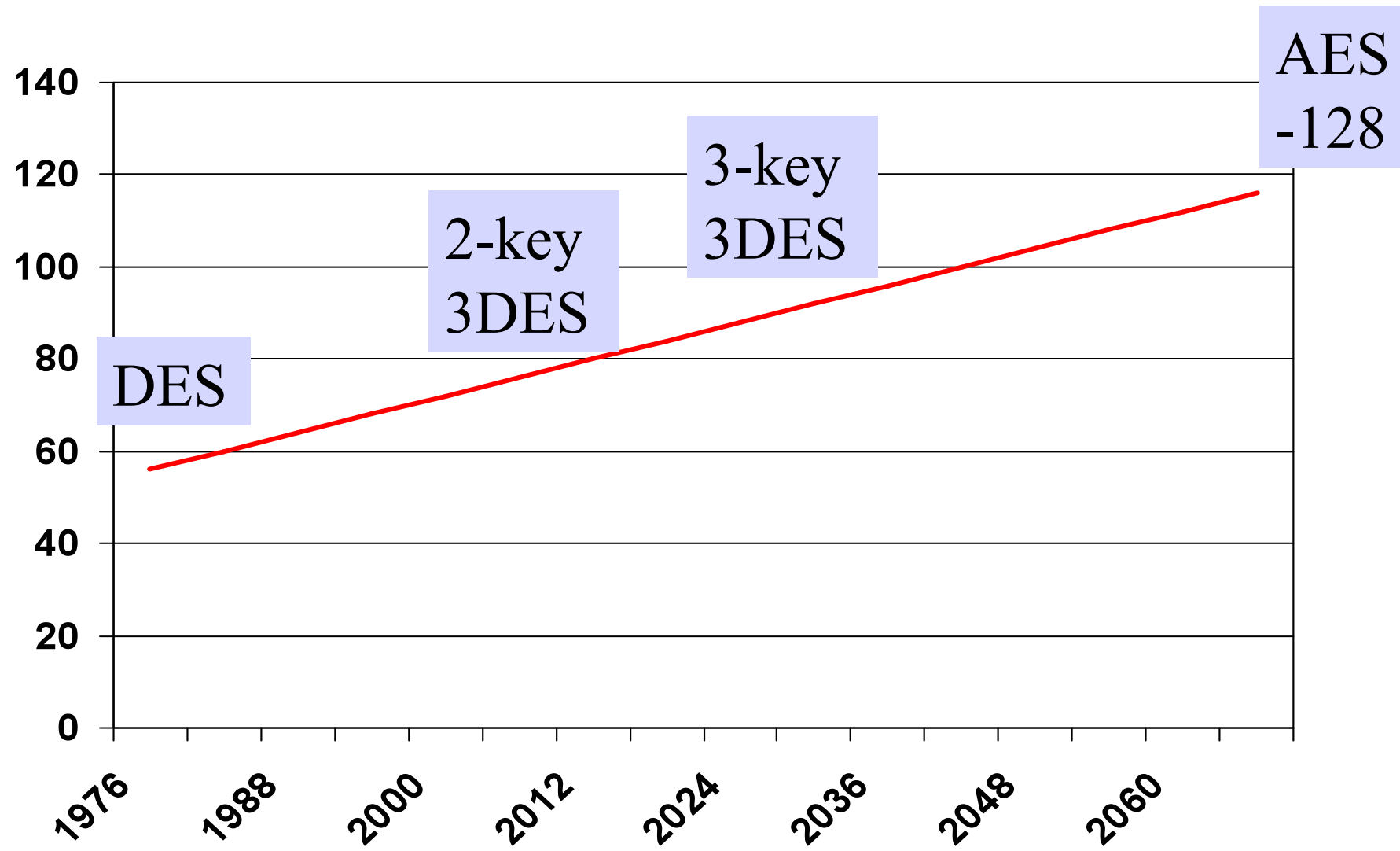
3-DES: NIST Spec. Pub. 800-67

(May 2004)

- two-key triple DES: until 2009
- three-key triple DES: until 2030



Symmetric Key Lengths and Moore's "law"



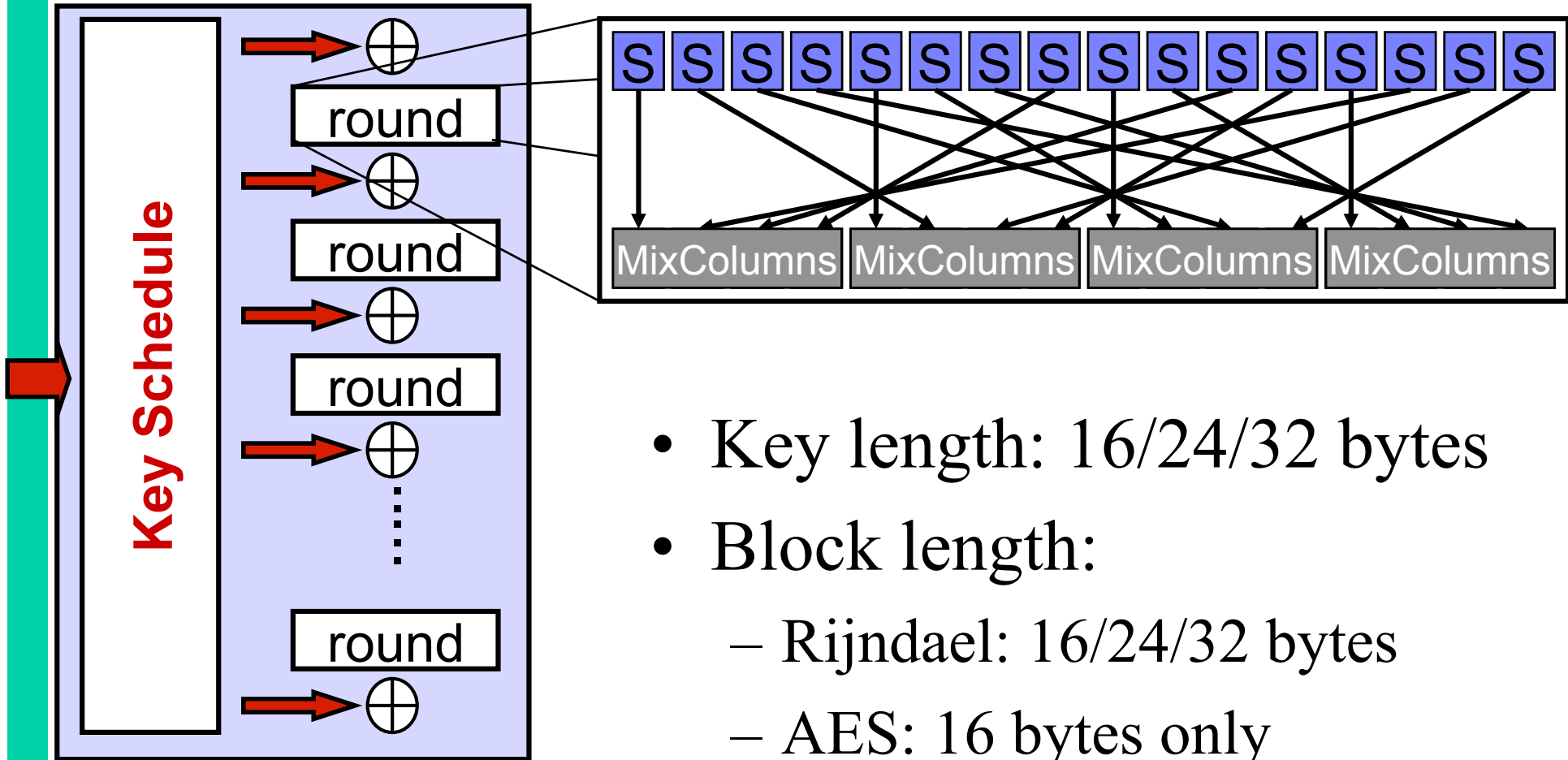
Moore's "law": speed of computers doubles every 18 months

AES (Advanced Encryption Standard)

- open competition launched by US government (Sept. '97) to replace DES
- 22 contenders including IBM, RSA, Deutsche Telekom
- 128-bit block cipher with key of 128/192/256 bits
- as strong as triple-DES, but more efficient
- royalty-free

A machine that cracks a DES key in 1 second would take 149 trillion years to crack a 128-bit key

AES: Rijndael



- Key length: 16/24/32 bytes
- Block length:
 - Rijndael: 16/24/32 bytes
 - AES: 16 bytes only

AES Status

- FIPS 197 published on Nov. 6, '01, effective May 26, '02
- mandatory for sensitive US govt. information
- mid 2003: AES-128 also for classified information and AES-192/-256 for *secret* and *top secret* information!
- fast adoption in the market (thousands of products)
 - Feb. 2010: 1290 AES product certifications by NIST <http://csrc.nist.gov/groups/STM/cavp/documents/aes/aesval.html>
 - standardization: ISO, IETF, IEEE 802.11,...
- slower adoption in financial sector
- software: 7.6 cycles/byte [Käsper-Schwabe'09]
- hardware: Intel will provide AES instruction (Westmere, 2010) at 0.75 cycles/byte for decryption



Encryption limitations

- Ciphertext becomes random string: “normal” crypto does not encrypt a credit card number into a (valid) credit card number
- Typically does not hide the length of the plaintext (unless randomized padding)
- Does **not** hide existence of plaintext (requires steganography)
- Does **not** hide that Alice is talking to Bob (requires traffic confidentiality)

Symmetric cryptology: data authentication

- the problem
- hash functions without a key
 - MDC: Manipulation Detection Codes
- hash functions with a secret key
 - MAC: Message Authentication Codes

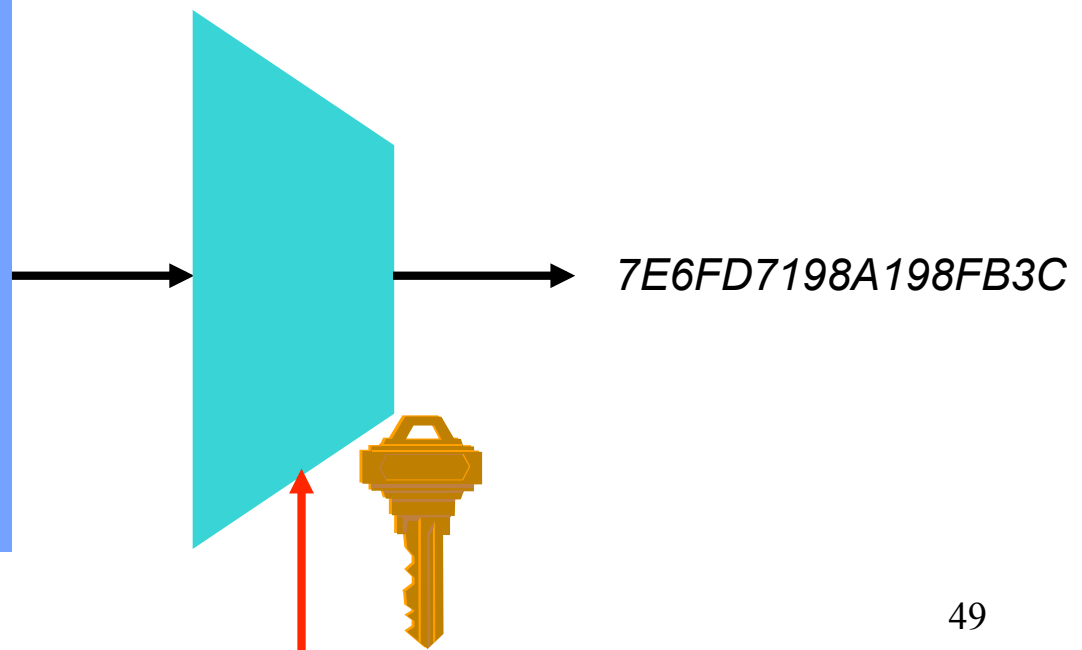
Data authentication: the problem

- encryption provides confidentiality:
 - prevents Eve from learning information on the cleartext/plaintext
 - but does not protect against modifications (active eavesdropping)
- Bob wants to know:
 - the **source** of the information (data origin)
 - that the information has not been **modified**
 - (optionally) **timeliness** and **sequence**
- data authentication is typically more complex than data confidentiality

Data authentication: MAC algorithms

- Replace protection of authenticity of (long) message by protection of secrecy of (short) key
 - Add MAC to the plaintext
- CBC-MAC
 - HMAC

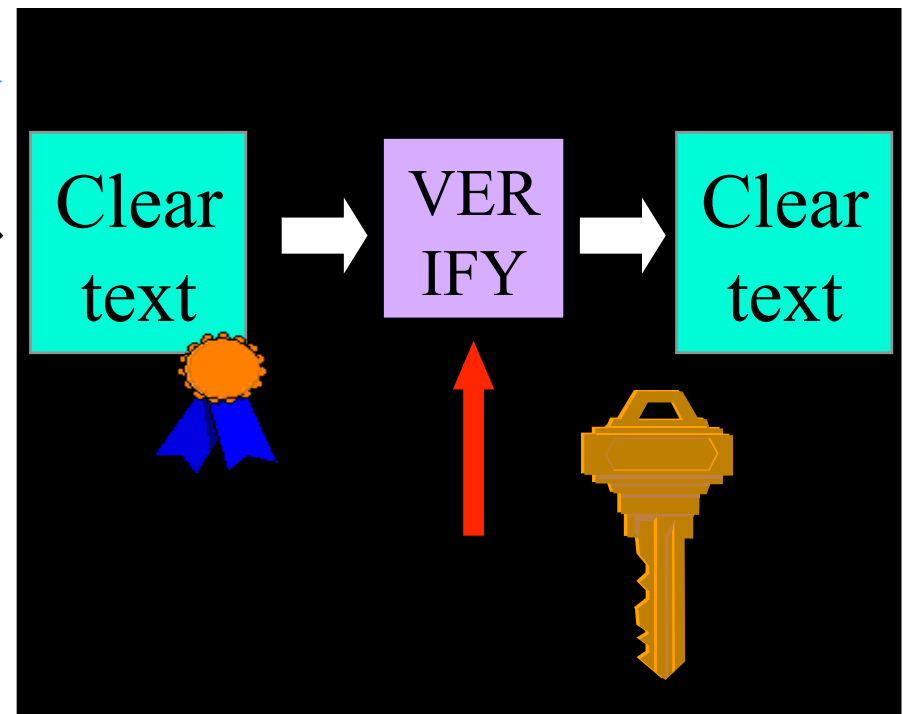
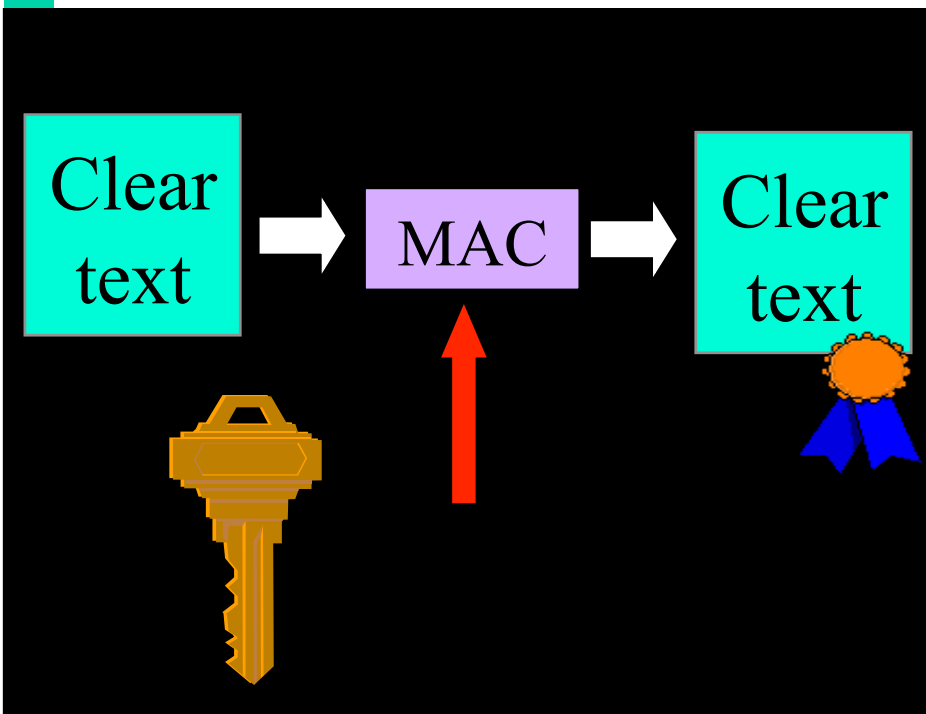
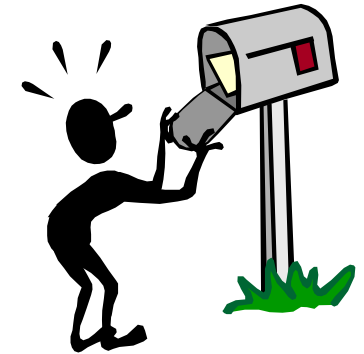
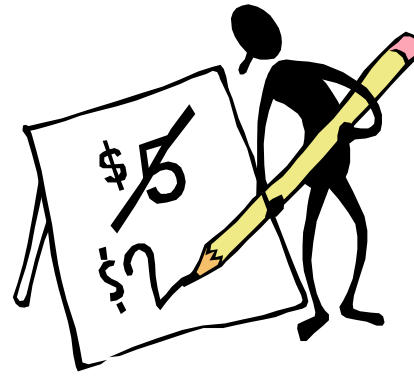
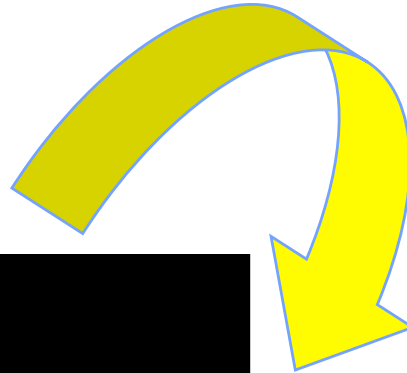
This is an input to a MAC algorithm. The input is a very long string, that is reduced by the hash function to a string of fixed length. There are additional security conditions: it should be very hard for someone who does not know the secret key to compute the hash function on a new input.



MAC algorithms



Modify



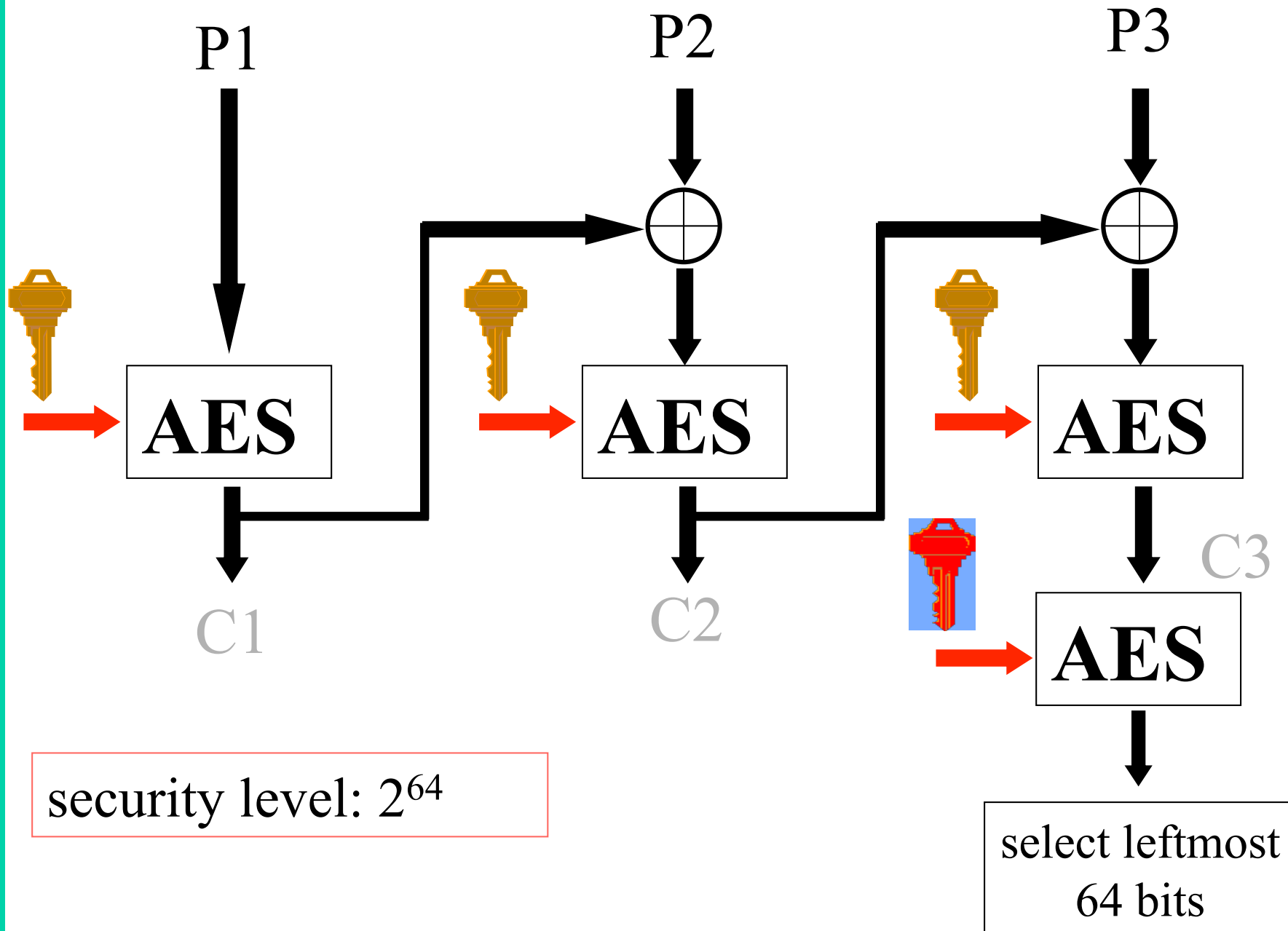
Data authentication: MAC algorithms

- typical MAC lengths: 32..96 bits
 - Forgery attacks: 2^m steps with m the MAC length in bits
- typical key lengths: (56)..112..160 bits
 - Exhaustive key search: 2^k steps with k the key length in bits
- birthday attacks: security level smaller than expected

MAC algorithms

- Banking: CBC-MAC based on triple-DES
- Internet: HMAC and CBC-MAC based on AES
- information theoretic secure MAC algorithms (authentication codes):
 - highly efficient
 - rather long keys
 - part of the key refreshed per message

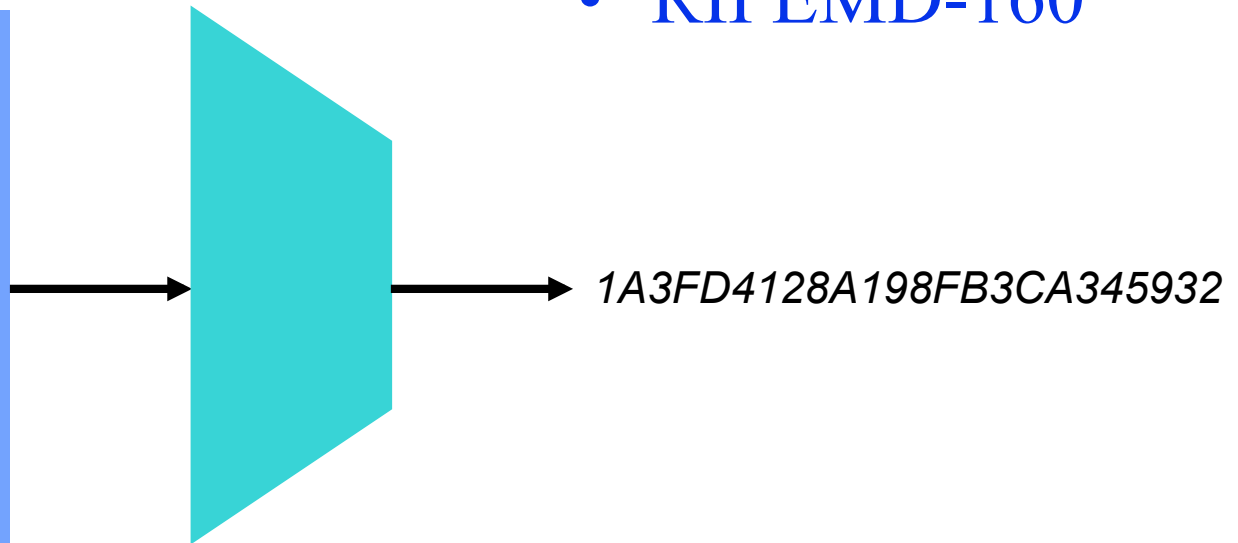
CBC-MAC based on AES



Data authentication: MDC

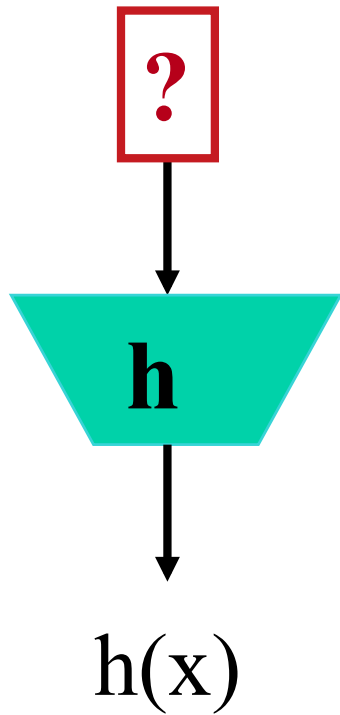
- MDC (manipulation detection code)
- Protect short hash value rather than long text
- (MD5)
- (SHA-1), SHA-256, SHA-512
- RIPEMD-160

This is an input to a cryptographic hash function. The input is a very long string, that is reduced by the hash function to a string of fixed length. There are additional security conditions: it should be very hard to find an input hashing to a given value (a preimage) or to find two colliding inputs (a collision).



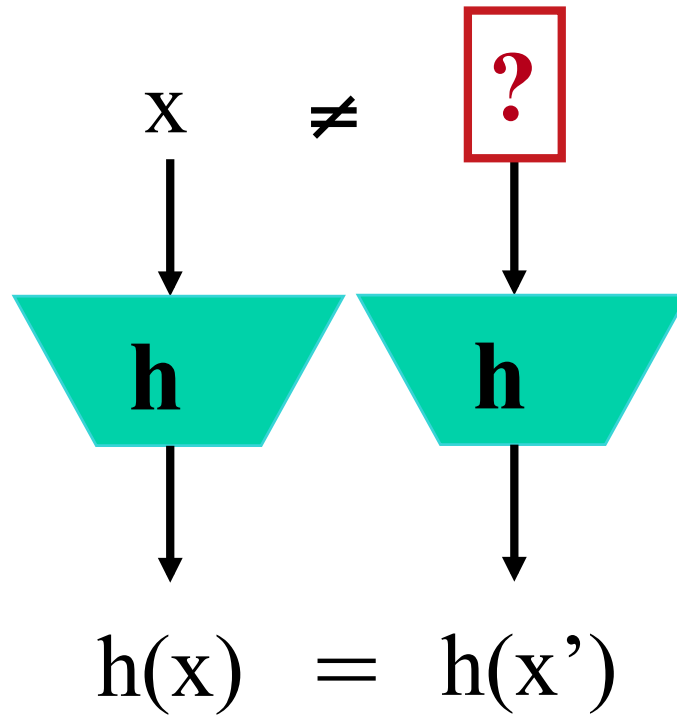
MDC Security requirements (n-bit result)

preimage



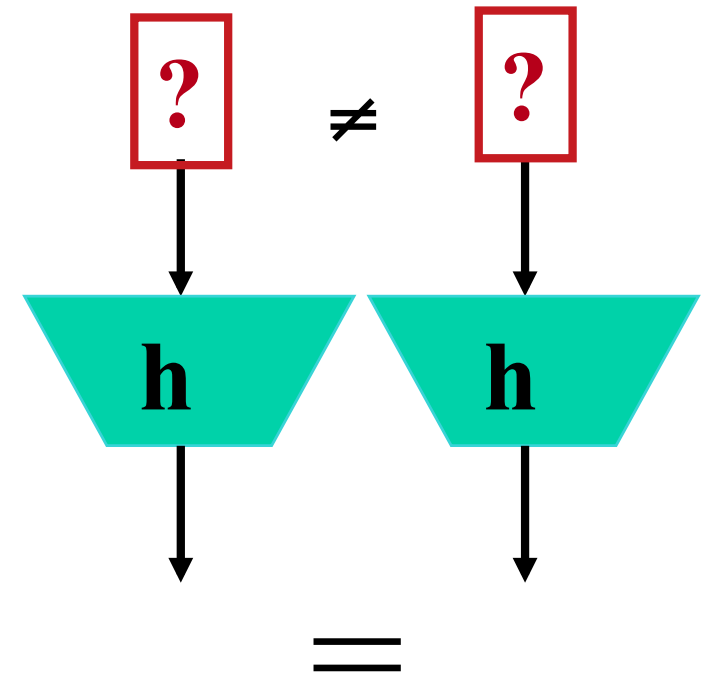
2^n

2nd preimage



2^n

collision



$2^{n/2}$

Data authentication: MDC

- n-bit result
- preimage resistance: for given y , hard to find input x such that $h(x) = y$ (2^n operations)
- 2nd preimage resistance: hard to find $x' \neq x$ such that $h(x') = h(x)$ (2^n operations)
- Collision resistance: hard to find (x, x') with $x' \neq x$ such that $h(x') = h(x)$ ($2^{n/2}$ operations)

MD5 and SHA-1

- SHA-1:
 - (2nd) preimage 2^{160} steps
 - collisions 2^{80} steps

60 M\$ for 1 year

Shortcut: Aug. 2007: 2^{60} steps

- MD5
 - (2nd) preimage 2^{128} steps
 - collisions 2^{64} steps

15 K\$ for 1 month

Shortcut: Aug. 2004: 2^{39} steps
(today: milliseconds)



Public-key cryptology

- the problem
- public-key encryption
- digital signatures
- an example: RSA
- advantages of public-key cryptology

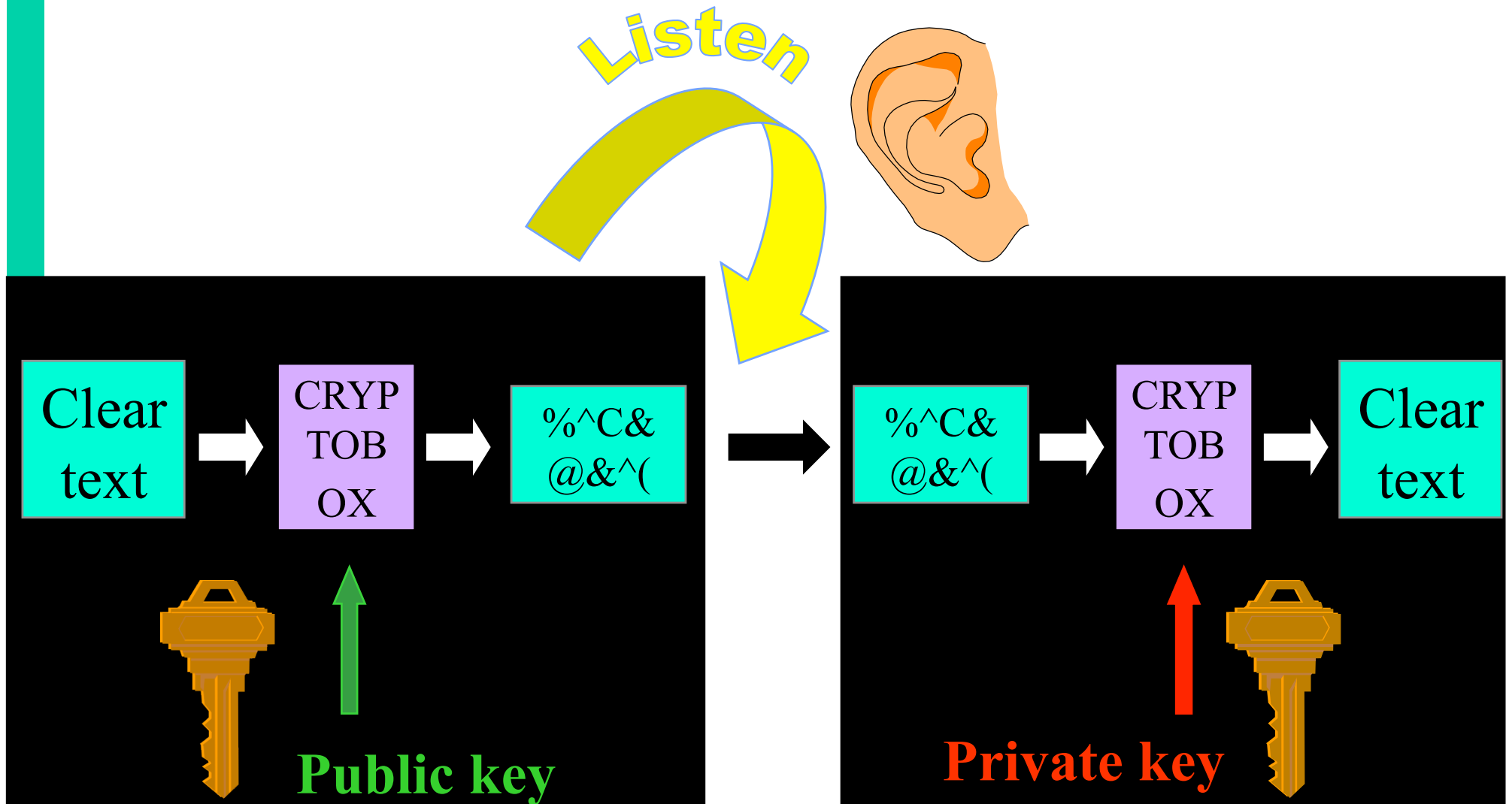
Limitation of symmetric cryptology

- Reduce security of information to security of keys

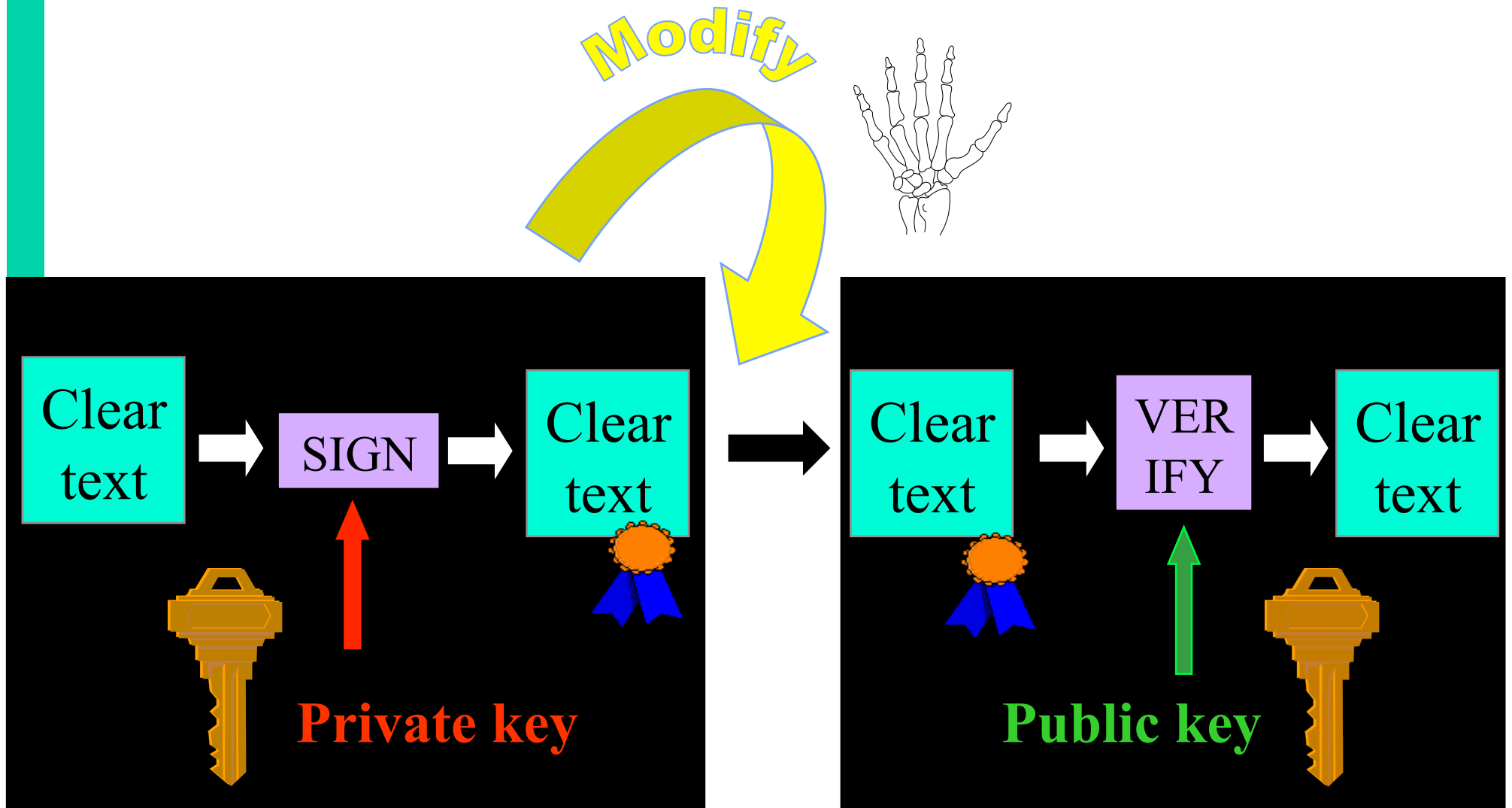


- But: how to establish these secret keys?
 - Cumbersome and expensive
 - Or risky: all keys in 1 place
- Do we really need to establish secret keys?

Public key cryptology: encryption

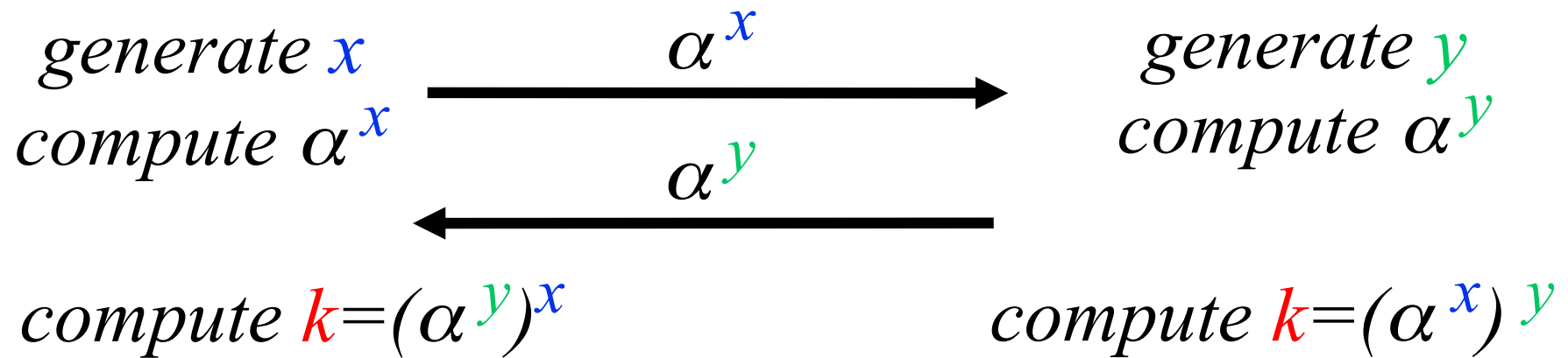


Public key cryptology: digital signature



A public-key distribution protocol: Diffie-Hellman

- Before: Alice and Bob have never met and share no secrets; they know a public system parameter α



- After: Alice and Bob share a short term key k
 - Eve cannot compute k : in several mathematical structures it is hard to derive x from α^x (this is known as the discrete logarithm problem)

RSA ('78)

- Choose 2 “large” prime numbers p and q
- modulus $n = p \cdot q$
- compute $\lambda(n) = \text{lcm}(p-1, q-1)$
- choose e relatively prime w.r.t. $\lambda(n)$
- compute $d = e^{-1} \pmod{\lambda(n)}$
- public key = (e, n)
- private key = d of (p, q)

The security of RSA is based on the “fact” that it is easy to generate two large primes, but that it is hard to factor their product

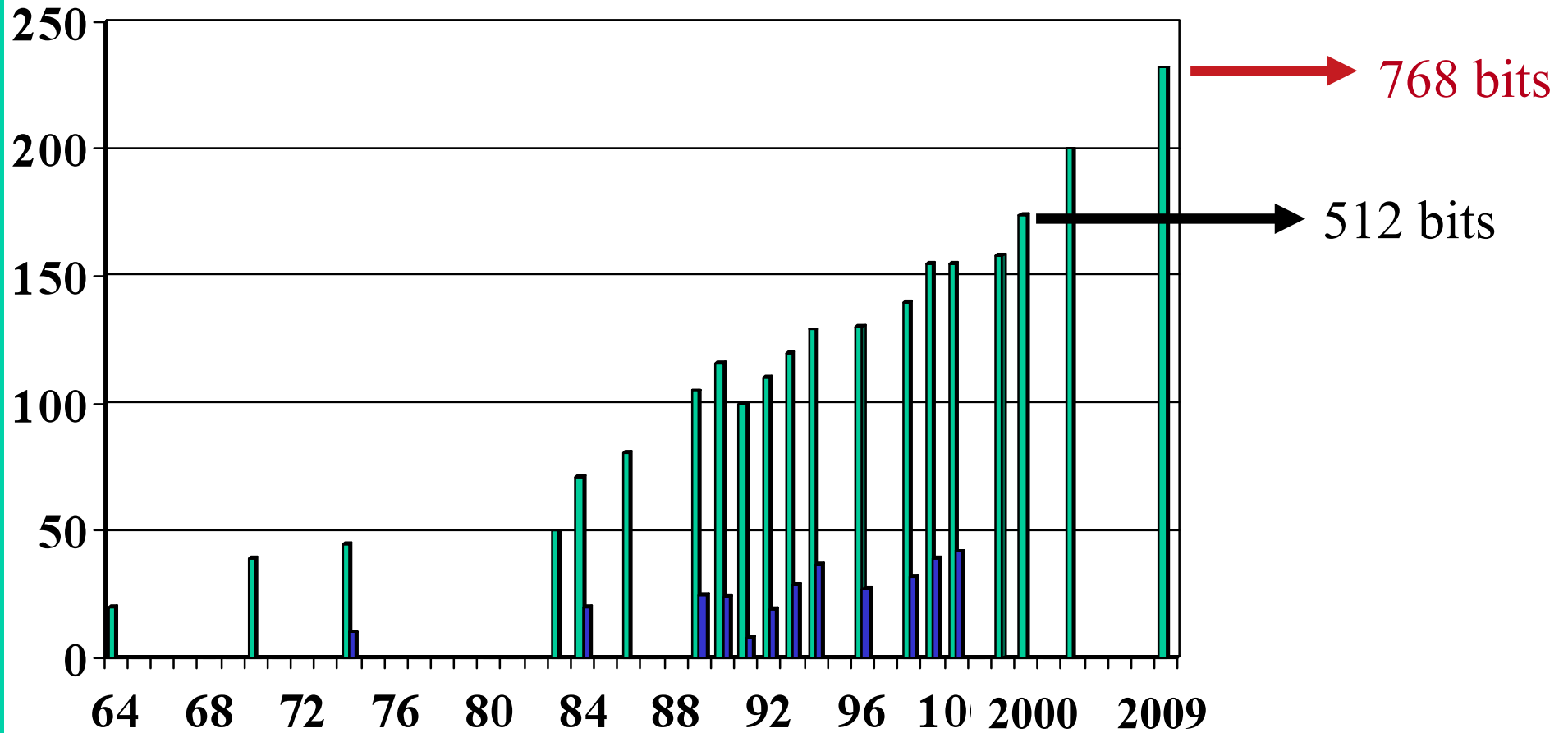
- encryption: $c = m^e \pmod n$
- decryption: $m = c^d \pmod n$

try to factor 2419

Factorisation records

2009: 768 bits or 232 digits

1 digit ~ 3.3 bits

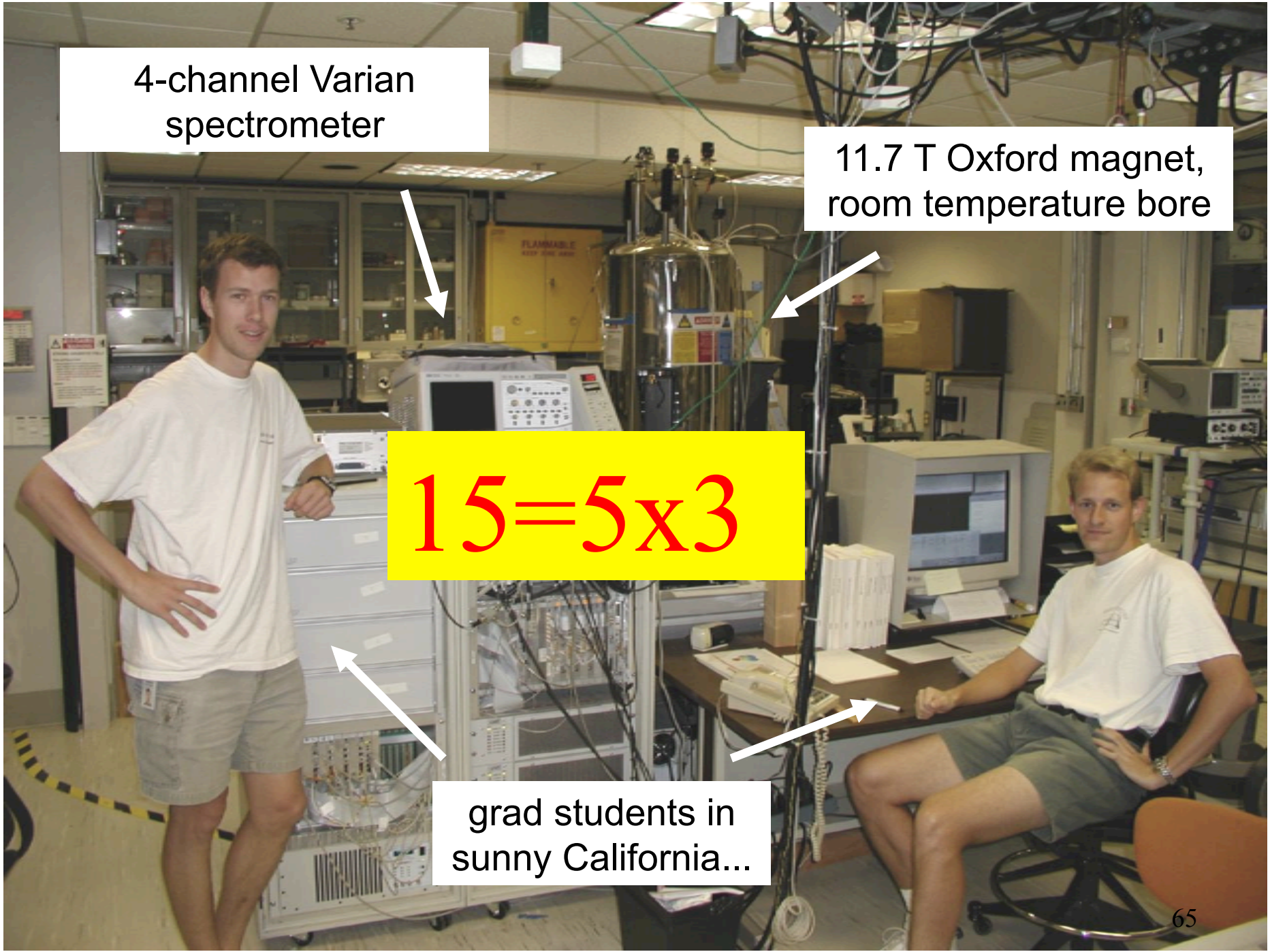


4-channel Varian spectrometer

11.7 T Oxford magnet, room temperature bore

15=5x3

grad students in sunny California...



Advantages of public key cryptology

- Reduce protection of information to protection of authenticity of public keys
- Confidentiality without establishing secret keys
 - extremely useful in an **open** environment
- Data authentication without shared secret keys: **digital signature**
 - sender and receiver have different capability
 - third party can resolve dispute between sender and receiver

Disadvantages of public key cryptology

- Calculations in software or hardware **two to three orders of magnitude** slower than symmetric algorithms
- Longer keys: 1024 bits rather than 56...128 bits
- What if factoring is easy?

Crypto software libraries

http://ece.gmu.edu/crypto_resources/web_resources/libraries.htm

C/C++/C#

- Botan (C++)
- Cryptlib
- Crypto++ (C++)
- Libgcrypt (C++)
- MatrixSSL (C++) embedded
- Miracl (binaries)
- OpenSSL (C++)
- BouncyCastle (BC#)

Java

- SunJCA/JCE
- BouncyCastle (BC)
- CryptixCrypto (until '05)
- EspreSSL
- FlexiProvider
- GNU Crypto
- IAIK
- Java SSL
- RSA JSafe

Reading material

- B. Preneel, Modern cryptology: an introduction.
 - This text corresponds more or less to the second half of these slides
 - It covers in more detail how block ciphers are used in practice, and explains how DES works.
 - It does not cover identification, key management and application to network security.

Selected books on cryptology

- D. Stinson, *Cryptography: Theory and Practice*, CRC Press, 3rd Ed., 2005. Solid introduction, but only for the mathematically inclined.
- A.J. Menezes, P.C. van Oorschot, S.A. Vanstone, *Handbook of Applied Cryptography*, CRC Press, 1997. The bible of modern cryptography. Thorough and complete reference work – not suited as a first text book. Freely available at <http://www.cacr.math.uwaterloo.ca/hac>
- N. Smart, *Cryptography, An Introduction*: 3rd Ed., 2008. Solid and up to date but on the mathematical side. Freely available at http://www.cs.bris.ac.uk/~nigel/Crypto_Book/
- B. Schneier, *Applied Cryptography*, Wiley, 1996. Widely popular and very accessible – make sure you get the errata.
- Other authors: Johannes Buchmann, Serge Vaudenay

Books on network security and more

- W. Stallings, *Network and Internetwork Security: Principles and Practice*, Prentice Hall, 5th Ed., November 2009. Solid background on network security. Explains basic concepts of cryptography. Tends to confuse terminology for decrypting and signing with RSA.
- Nagand Doraswamy, Dan Harkins, *IPsec - The New Security Standard for the Internet, Intranets, and Virtual Private Networks*, Prentice Hall, 1999. A well written overview of the IPsec protocol (but now outdated).
- W. Diffie, S. Landau, *Privacy on the line. The politics of wiretapping and encryption*, MIT Press, 2007. The best book so far on the intricate politics of the field.

More information: some links

- IACR (International Association for Cryptologic Research): www.iacr.org
- IETF web site: www.ietf.org
- Cryptography faq: www.faqs.org/faqs/cryptography-faq
- Counterpane links: www.counterpane.com/hotlist.html
- Digicrime (www.digicrime.org) - not serious but informative and entertaining